



CS 380 - GPU and GPGPU Programming Lecture 16: GPU Texturing, Pt. 3

Markus Hadwiger, KAUST

Reading Assignment #10 (until Nov 8)



Read (required):

• Brook for GPUs: Stream Computing on Graphics Hardware lan Buck et al., SIGGRAPH 2004

http://graphics.stanford.edu/papers/brookgpu/

Read (optional):

• The Imagine Stream Processor Ujval Kapasi et al.; IEEE ICCD 2002

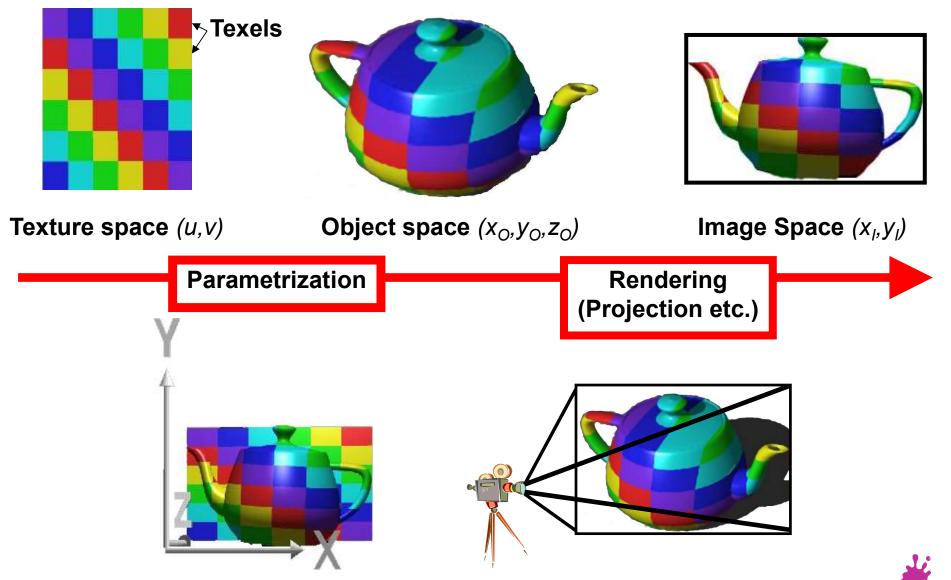
http://cva.stanford.edu/publications/2002/imagine-overview-iccd/

• Merrimac: Supercomputing with Streams Bill Dally et al.; SC 2003

https://dl.acm.org/citation.cfm?doid=1048935.1050187

Texturing: General Approach





Eduard Gröller, Stefan Jeschke

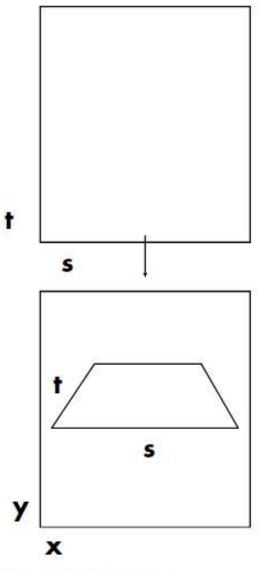


Interpolation Type + Purpose #1: Interpolation of Texture Coordinates

(Linear / Rational-Linear Interpolation)

Texture Mapping

2D (3D) Texture Space **Texture Transformation** 2D Object Parameters Parameterization 3D Object Space **Model Transformation** 3D World Space **Viewing Transformation 3D Camera Space** Projection 2D Image Space



Kurt Akeley, Pat Hanrahan

Perspective-Correct Interpolation Recipe

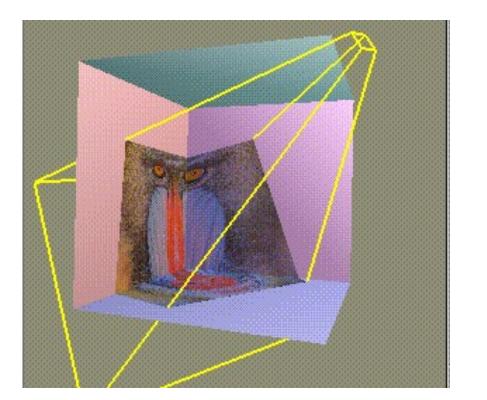


$$r_i(x,y) = \frac{r_i(x,y)/w(x,y)}{1/w(x,y)}$$

- (1) Associate a record containing the *n* parameters of interest (r_1, r_2, \dots, r_n) with each vertex of the polygon.
- (2) For each vertex, transform object space coordinates to homogeneous screen space using 4×4 object to screen matrix, yielding the values (xw, yw, zw, w).
- (3) Clip the polygon against plane equations for each of the six sides of the viewing frustum, linearly interpolating all the parameters when new vertices are created.
- (4) At each vertex, divide the homogeneous screen coordinates, the parameters r_i , and the number 1 by w to construct the variable list $(x, y, z, s_1, s_2, \dots, s_{n+1})$, where $s_i = r_i/w$ for $i \leq n$, $s_{n+1} = 1/w$.
- (5) Scan convert in screen space by linear interpolation of all parameters, at each pixel computing r_i = s_i/s_{n+1} for each of the n parameters; use these values for shading.
 Heckbert and Moreton

Projective Texture Mapping

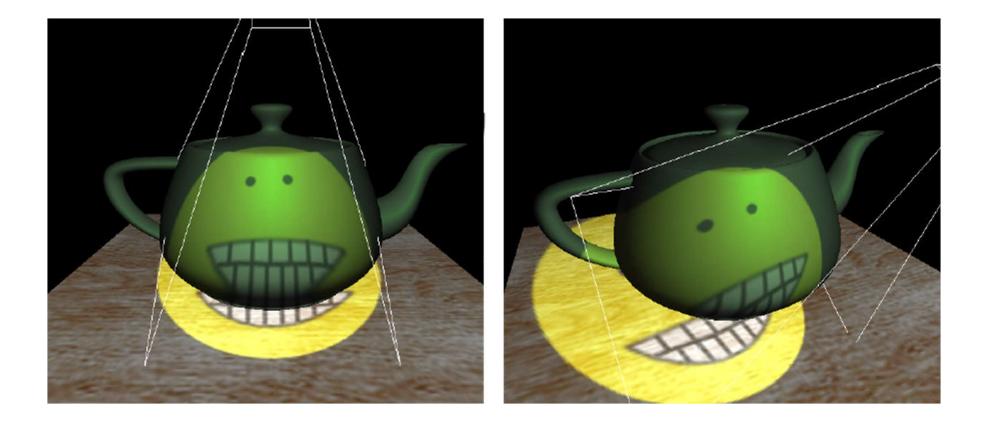
- Want to simulate a beamer
 - ... or a flashlight, or a slide projector
- Precursor to shadows
- Interesting mathematics:
 2 perspective
 projections involved!
- Easy to program!





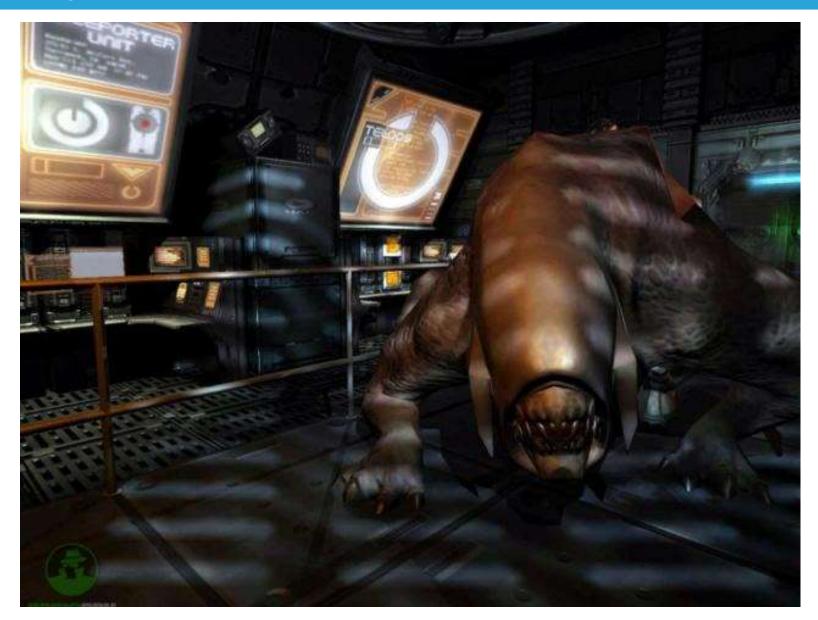
Projective Texture Mapping





Projective Shadows in Doom 3







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Projective Texturing



- What about homogeneous texture coords?
- Need to do perspective divide also for projector!
 - (s, t, q) \rightarrow (s/q, t/q) for every fragment
- How does OpenGL do that?
 - Needs to be perspective correct as well!
 - Trick: interpolate (s/w, t/w, r/w, q/w)
 - (s/w) / (q/w) = s/q etc. at every fragment
- Remember: s,t,r,q are equivalent to x,y,z,w in projector space! → r/q = projector depth!





- Apply multiple textures in one pass
- Integral part of programmable shading
 - e.g. diffuse texture map + gloss map
 - e.g. diffuse texture map + light map
- Performance issues
 - How many textures are free?
 - How many are available









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Example: Light Mapping

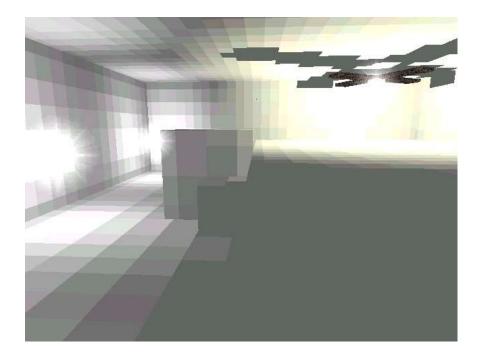


- Used in virtually every commercial game
- Precalculate diffuse lighting on static objects
 - Only low resolution necessary
 - Diffuse lighting is view independent!
- Advantages:
 - No runtime lighting necessary
 - VERY fast!
 - Can take global effects (shadows, color bleeds) into account



Light Mapping







Original LM texels

Bilinear Filtering

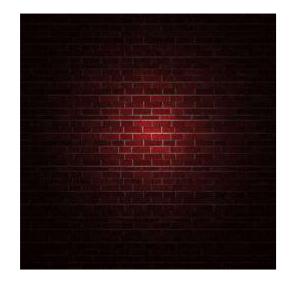


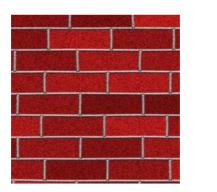
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Why premultiplication is bad...







Full Size Texture (with Lightmap)

Tiled Surface Texture plus Lightmap

 \rightarrow use tileable surface textures and low resolution lightmaps



Light Mapping





Original scene



Light-mapped



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Example: Light Mapping

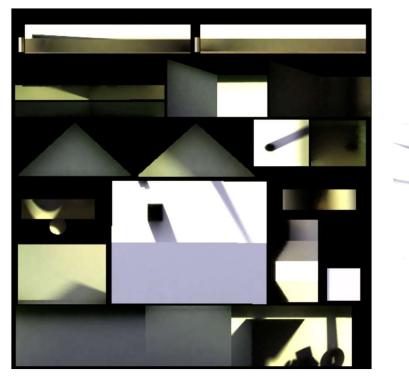


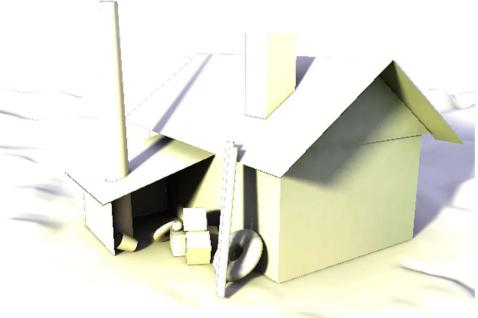
- Precomputation based on non-realtime methods
 - Radiosity
 - Ray tracing
 - Monte Carlo Integration
 - Path tracing
 - Photon mapping



Light Mapping







Lightmap

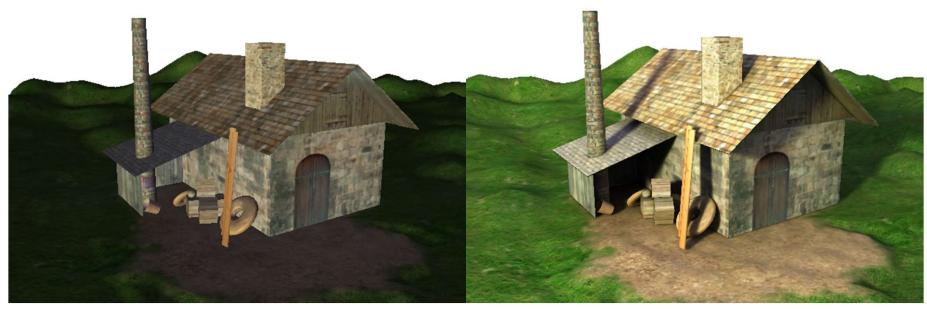
mapped



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Light Mapping





Original scene

Light-mapped



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Interpolation Type + Purpose #2: Interpolation of Samples in Texture Space

(Multi-Linear Interpolation)

Types of Textures



- Spatial layout
 - Cartesian grids: 1D, 2D, 3D, 2D_ARRAY, …
 - Cube maps, …
- Formats (too many), e.g. OpenGL
 - GL_LUMINANCE16_ALPHA16
 - GL_RGB8, GL_RGBA8, …: integer texture formats
 - GL_RGB16F, GL_RGBA32F, ...: float texture formats
 - compressed formats, high dynamic range formats, …
- External (CPU) format vs. internal (GPU) format
 - OpenGL driver converts from external to internal



Magnification (Bi-linear Filtering Example)





Original image





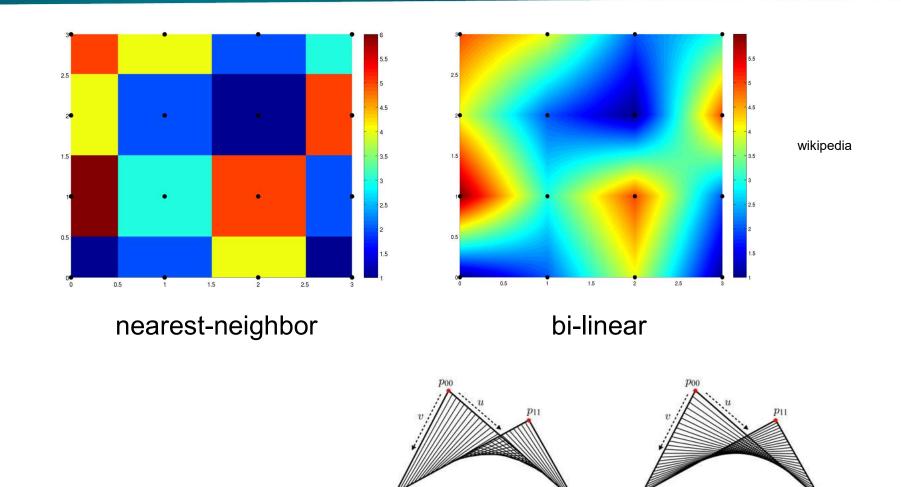


Bi-linear filtering



Nearest-Neighbor vs. Bi-Linear Interpolation





Markus Hadwiger

 p_{01}

P10

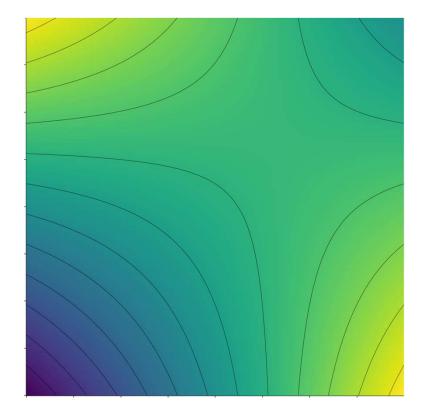
Bilinear patch (courtesy J. Han)

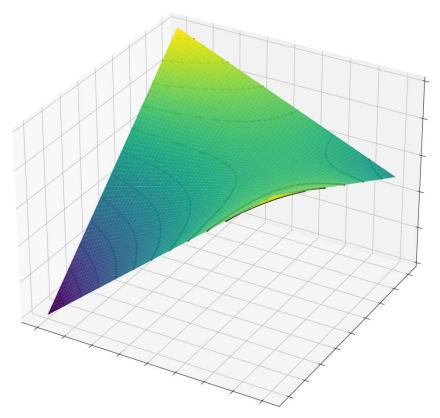
 p_{01}



Consider area between 2x2 adjacent samples (e.g., pixel centers)

Example #2: 1 at top-left and bottom-right, 0 at bottom-left, 0.5 at top-right







Consider area between 2x2 adjacent samples (e.g., pixel centers):

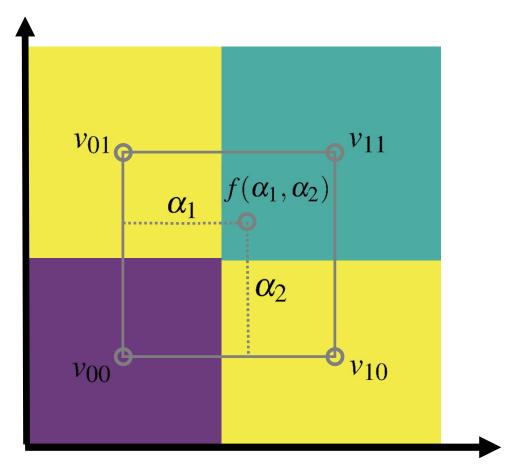
Given any (fractional) position

$\alpha_1 := x_1 - \lfloor x_1 \rfloor$	$\alpha_1 \in [0.0, 1.0)$
$\alpha_2 := x_2 - \lfloor x_2 \rfloor$	$lpha_2 \in [0.0, 1.0)$

and 2x2 sample values

$$\begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix}$$

Compute: $f(\alpha_1, \alpha_2)$





Consider area between 2x2 adjacent samples (e.g., pixel centers):

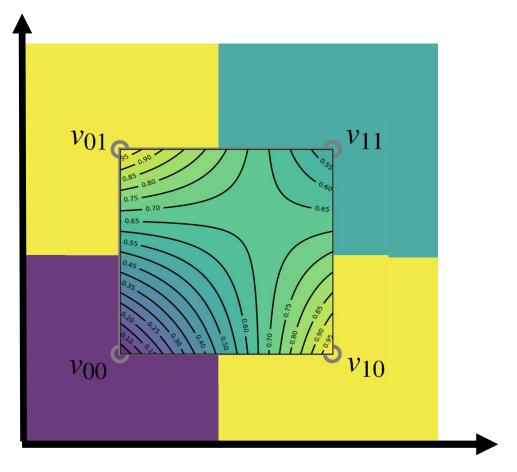
Given any (fractional) position

$\alpha_1 := x_1 - \lfloor x_1 \rfloor$	$\alpha_1 \in [0.0, 1.0)$
$\alpha_2 := x_2 - \lfloor x_2 \rfloor$	$lpha_2 \in [0.0, 1.0)$

and 2x2 sample values

$$\begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix}$$

Compute: $f(\alpha_1, \alpha_2)$





Weights in 2x2 format:

$$\begin{bmatrix} \alpha_2 \\ (1-\alpha_2) \end{bmatrix} \begin{bmatrix} (1-\alpha_1) & \alpha_1 \end{bmatrix} = \begin{bmatrix} (1-\alpha_1)\alpha_2 & \alpha_1\alpha_2 \\ (1-\alpha_1)(1-\alpha_2) & \alpha_1(1-\alpha_2) \end{bmatrix}$$

Interpolate function at (fractional) position (α_1, α_2):

$$f(\boldsymbol{\alpha}_1, \boldsymbol{\alpha}_2) = \begin{bmatrix} \boldsymbol{\alpha}_2 & (1 - \boldsymbol{\alpha}_2) \end{bmatrix} \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \boldsymbol{\alpha}_1) \\ \boldsymbol{\alpha}_1 \end{bmatrix}$$



Interpolate function at (fractional) position (α_1, α_2):

$$f(\boldsymbol{\alpha}_1, \boldsymbol{\alpha}_2) = \begin{bmatrix} \boldsymbol{\alpha}_2 & (1 - \boldsymbol{\alpha}_2) \end{bmatrix} \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \boldsymbol{\alpha}_1) \\ \boldsymbol{\alpha}_1 \end{bmatrix}$$

$$= \begin{bmatrix} \alpha_2 & (1 - \alpha_2) \end{bmatrix} \begin{bmatrix} (1 - \alpha_1)v_{01} + \alpha_1v_{11} \\ (1 - \alpha_1)v_{00} + \alpha_1v_{10} \end{bmatrix}$$

$$= \begin{bmatrix} \alpha_2 v_{01} + (1 - \alpha_2) v_{00} & \alpha_2 v_{11} + (1 - \alpha_2) v_{10} \end{bmatrix} \begin{bmatrix} (1 - \alpha_1) \\ \alpha_1 \end{bmatrix}$$



Interpolate function at (fractional) position (α_1, α_2):

$$f(\boldsymbol{\alpha}_1, \boldsymbol{\alpha}_2) = \begin{bmatrix} \boldsymbol{\alpha}_2 & (1 - \boldsymbol{\alpha}_2) \end{bmatrix} \begin{bmatrix} v_{01} & v_{11} \\ v_{00} & v_{10} \end{bmatrix} \begin{bmatrix} (1 - \boldsymbol{\alpha}_1) \\ \boldsymbol{\alpha}_1 \end{bmatrix}$$

$$= (1 - \alpha_1)(1 - \alpha_2)v_{00} + \alpha_1(1 - \alpha_2)v_{10} + (1 - \alpha_1)\alpha_2v_{01} + \alpha_1\alpha_2v_{11}$$

$$= v_{00} + \alpha_1(v_{10} - v_{00}) + \alpha_2(v_{01} - v_{00}) + \alpha_1\alpha_2(v_{00} + v_{11} - v_{10} - v_{01})$$



REALLY IMPORTANT:

this is a different thing (for a different purpose) than the linear (or, in perspective, rational-linear) interpolation of texture coordinates!!



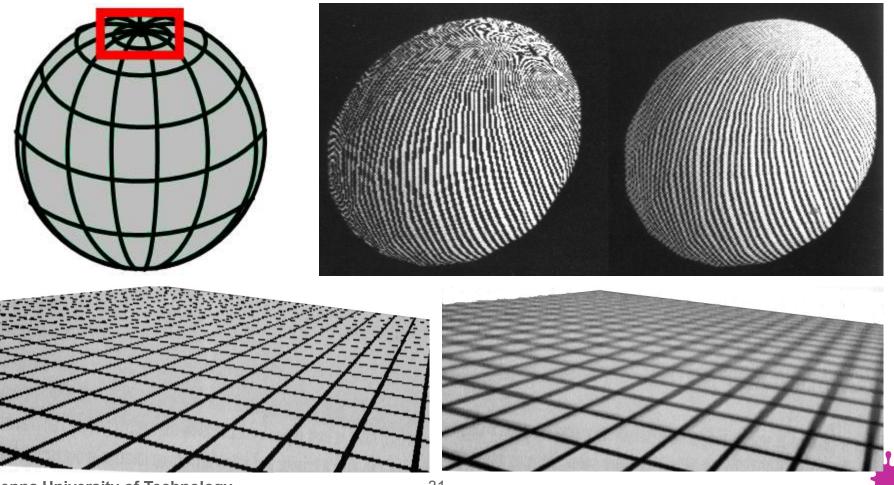
Texture Minification

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Texture Aliasing: Minification



Problem: One pixel in image space covers many texels

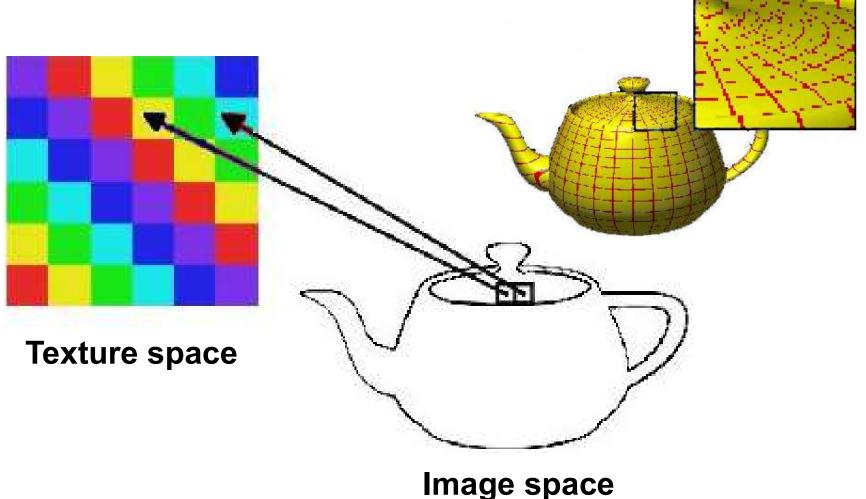


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Texture Aliasing: Minification



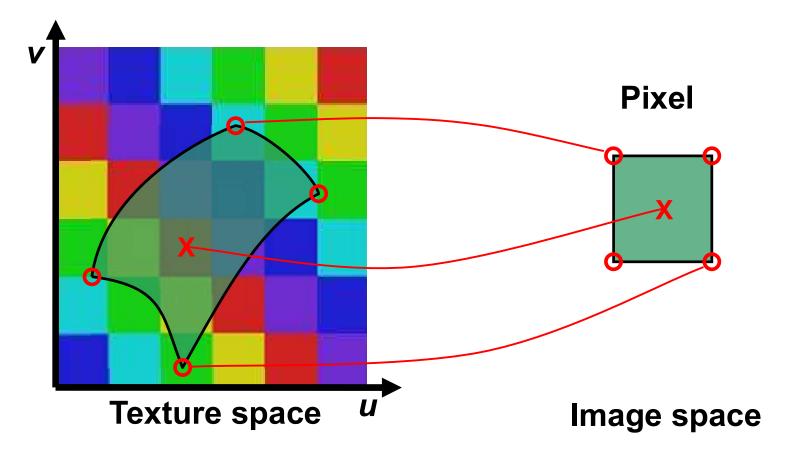
Caused by undersampling: texture information is lost



Texture Anti-Aliasing: Minification



A good pixel value is the weighted mean of the pixel area projected into texture space

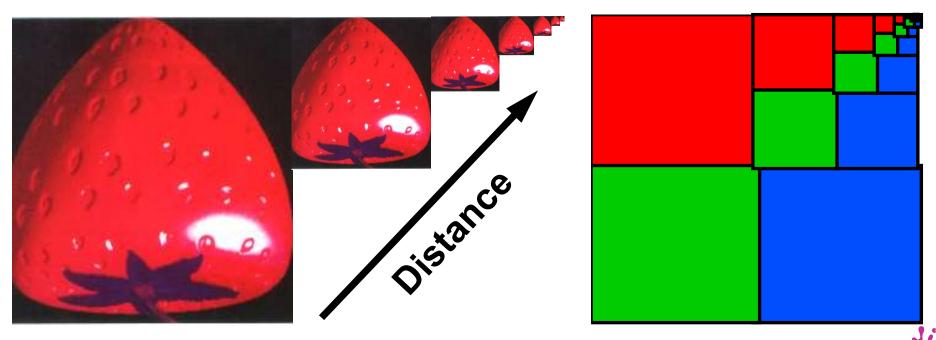




Texture Anti-Aliasing: MIP Mapping



- MIP Mapping ("Multum In Parvo")
 - Texture size is reduced by factors of 2 (downsampling = "many things in a small place")
 - Simple (4 pixel average) and memory efficient
 - Last image is only ONE texel



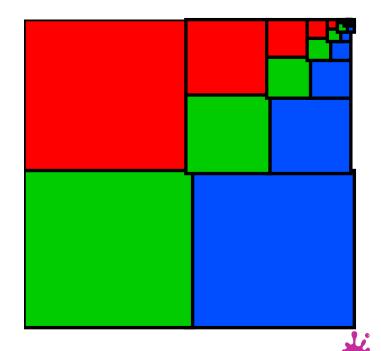




- MIP Mapping ("Multum In Parvo")
 - Texture size is reduced by factors of 2 (*downsampling* = "many things in a small place")
 - Simple (4 pixel average) and memory efficient
 - Last image is only ONE texel

geometric series:

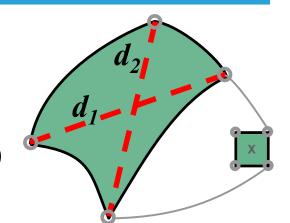
$$a + ar + ar^2 + ar^3 + \dots + ar^{n-1} = \ = \sum_{k=0}^{n-1} ar^k = a\left(rac{1-r^n}{1-r}
ight)$$

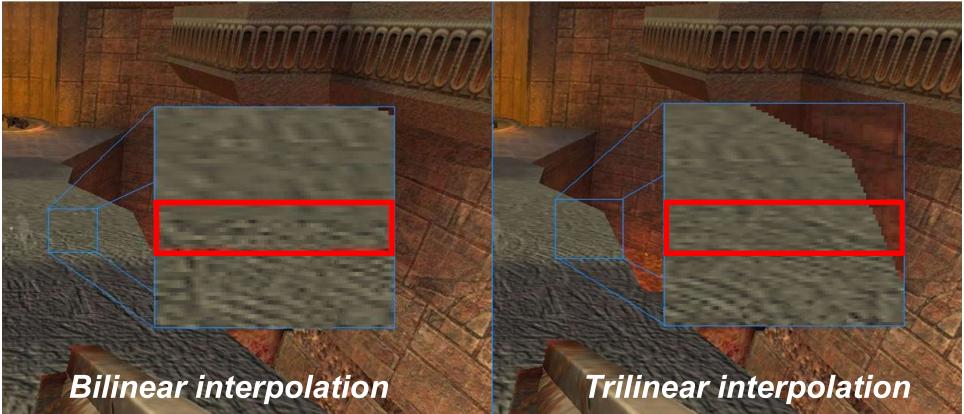


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Texture Anti-Aliasing: MIP Mapping

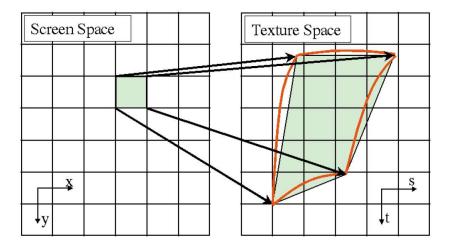
- MIP Mapping Algorithm
- $D := ld(max(d_1, d_2))$ "Mip Map level"
- $T_0 :=$ value from texture $D_0^{\bullet} = trunc$ (D)
 - Use bilinear interpolation

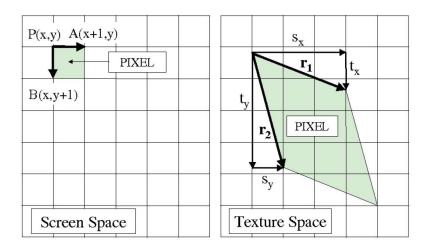




MIP-Map Level Computation







- Use the partial derivatives of texture coordinates with respect to screen space coordinates
- This is the Jacobian matrix

$$\begin{pmatrix} \frac{\partial u}{\partial x} & \frac{\partial u}{\partial y} \\ \frac{\partial v}{\partial x} & \frac{\partial v}{\partial y} \end{pmatrix} = \begin{pmatrix} s_{x} & s_{y} \\ t_{x} & t_{y} \end{pmatrix}$$

• Area of parallelogram is the absolute value of the Jacobian determinant (the Jacobian)

MIP-Map Level Computation (OpenGL)

• OpenGL 4.6 core specification, pp. 251-264

(3D tex coords!)

$$\lambda_{base}(x,y) = \log_2[\rho(x,y)]$$

$$\rho = \max\left\{\sqrt{\left(\frac{\partial u}{\partial x}\right)^2 + \left(\frac{\partial v}{\partial x}\right)^2 + \left(\frac{\partial w}{\partial x}\right)^2}, \sqrt{\left(\frac{\partial u}{\partial y}\right)^2 + \left(\frac{\partial v}{\partial y}\right)^2 + \left(\frac{\partial w}{\partial y}\right)^2}\right\}$$

Does not use area of parallelogram but greater hypotenuse [Heckbert, 1983]

• Approximation without square-roots

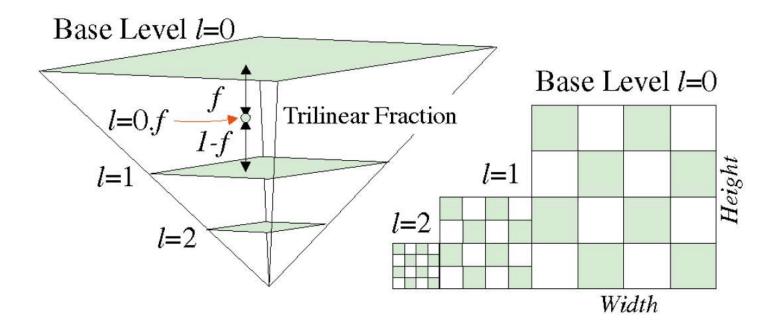
$$m_u = \max\left\{ \left| \frac{\partial u}{\partial x} \right|, \left| \frac{\partial u}{\partial y} \right| \right\} \quad m_v = \max\left\{ \left| \frac{\partial v}{\partial x} \right|, \left| \frac{\partial v}{\partial y} \right| \right\} \quad m_w = \max\left\{ \left| \frac{\partial w}{\partial x} \right|, \left| \frac{\partial w}{\partial y} \right| \right\}$$

$$\max\{m_u, m_v, m_w\} \le f(x, y) \le m_u + m_v + m_w$$

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MIP-Map Level Interpolation



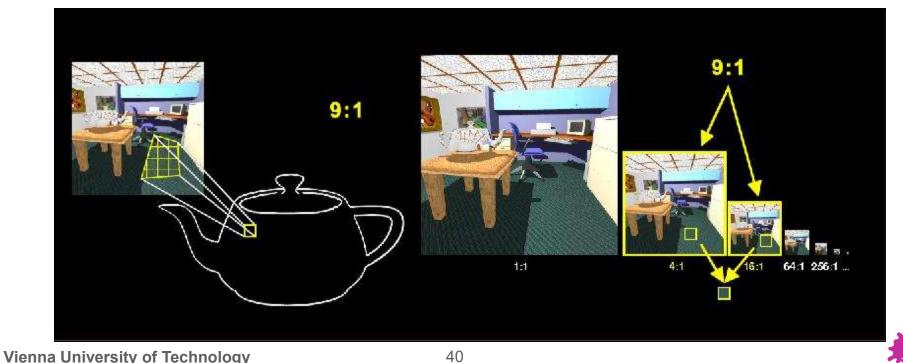


- Level of detail value is fractional!
- Use fractional part to blend (lin.) between two adjacent mipmap levels

Texture Anti-Aliasing: MIP Mapping



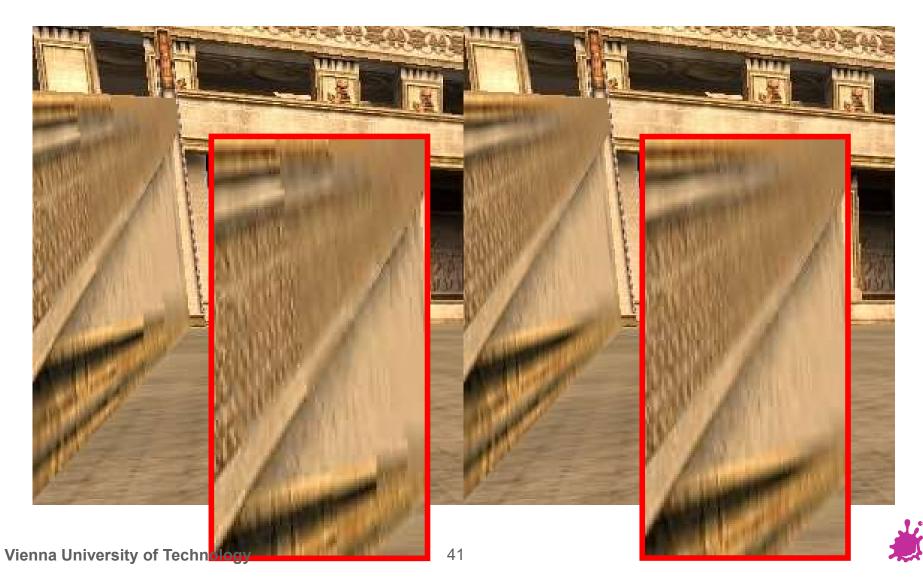
- Trilinear interpolation:
 - T₁ := value from texture $D_1 = D_0 + 1$ (bilin.interpolation)
 - Pixel value := $(D_1 D) \cdot T_0 + (D D_0) \cdot T_1$
 - Linear interpolation between successive MIP Maps
 - Avoids "Mip banding" (but doubles texture lookups)



Texture Anti-Aliasing: MIP Mapping



Other example for bilinear vs. trilinear filtering



Thank you.