

# **CS 247 – Scientific Visualization**

## **Lecture 14: Volume Visualization, Pt. 1**

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# Reading Assignment #8 (until Mar 23)



## Read (required):

- Real-Time Volume Graphics, Chapter 1  
(*Theoretical Background and Basic Approaches*),  
from beginning to 1.4.4 (inclusive)

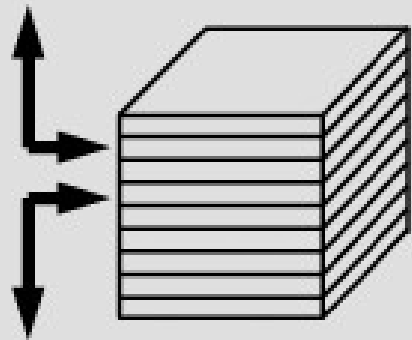
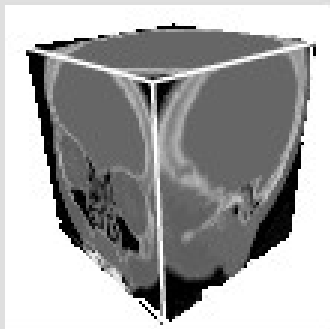
## Read (optional):

- Paper:  
*Nelson Max, Optical Models for Direct Volume Rendering,*  
*IEEE Transactions on Visualization and Computer Graphics, 1995*  
<http://dx.doi.org/10.1109/2945.468400>

# Volume Rendering

# Theory

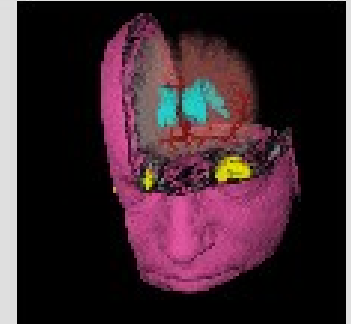
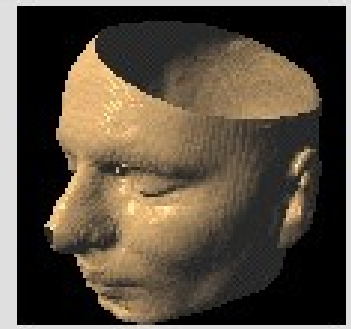
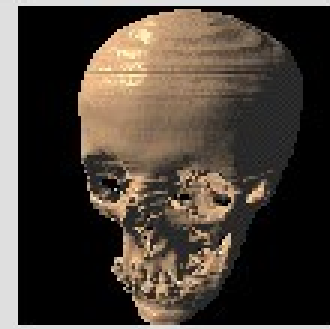
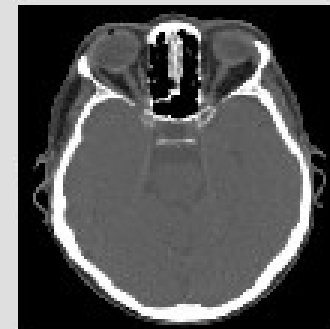
# Volume Visualization



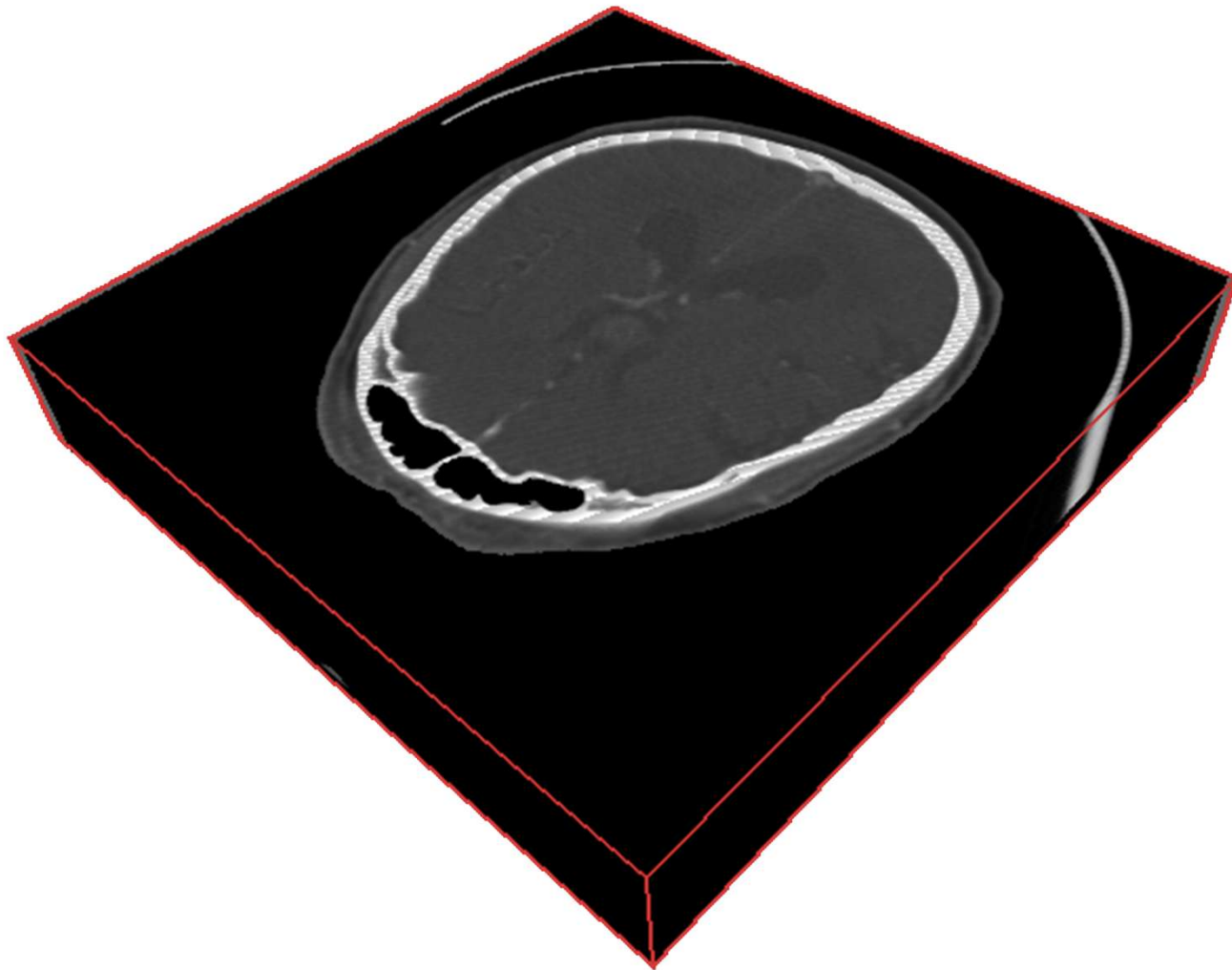
• 2D visualization slice images (or multi-planar reformatting MPR)

• *Indirect* 3D visualization isosurfaces (or surface-shaded display: SSD)

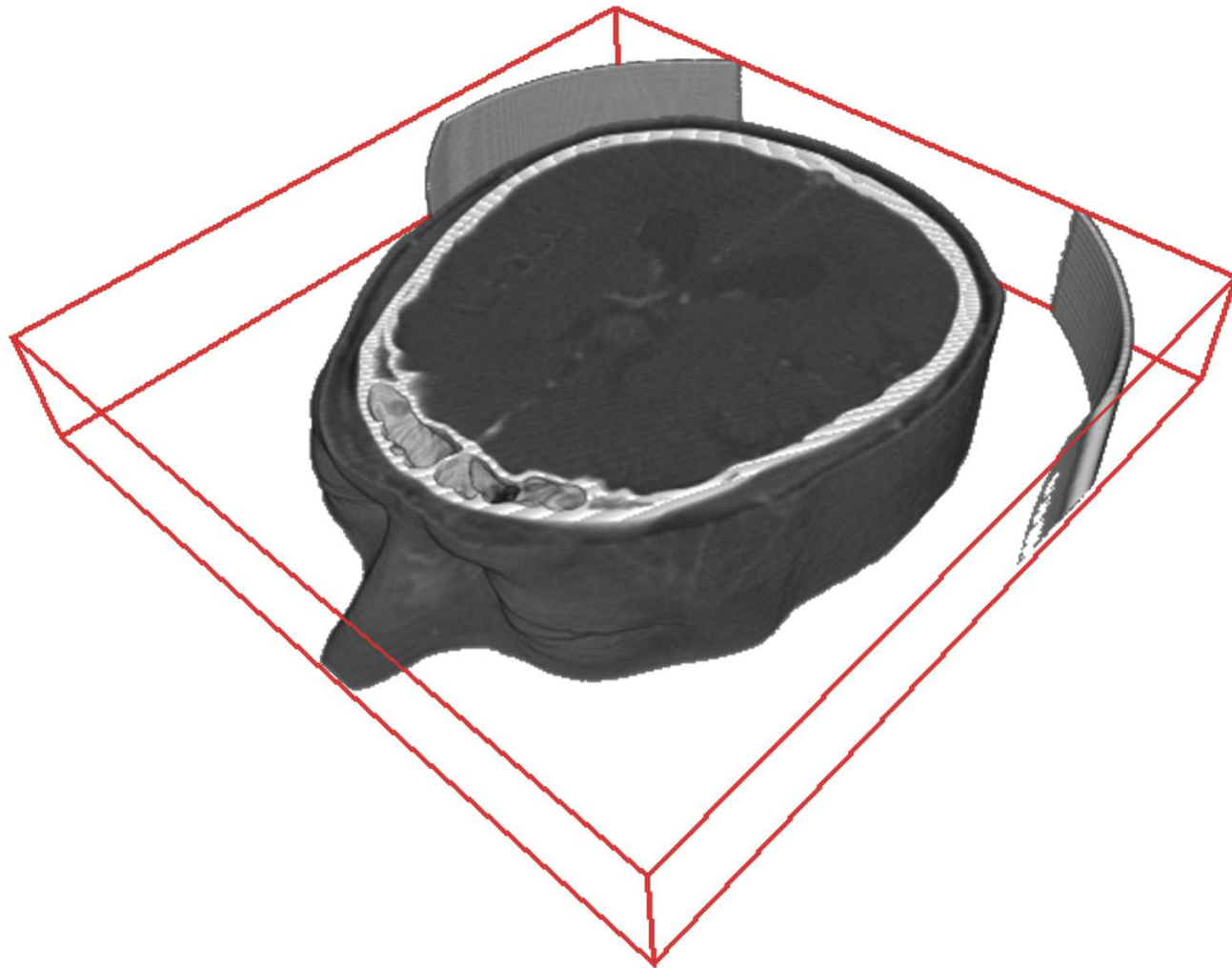
• *Direct* 3D visualization (direct volume rendering: DVR)



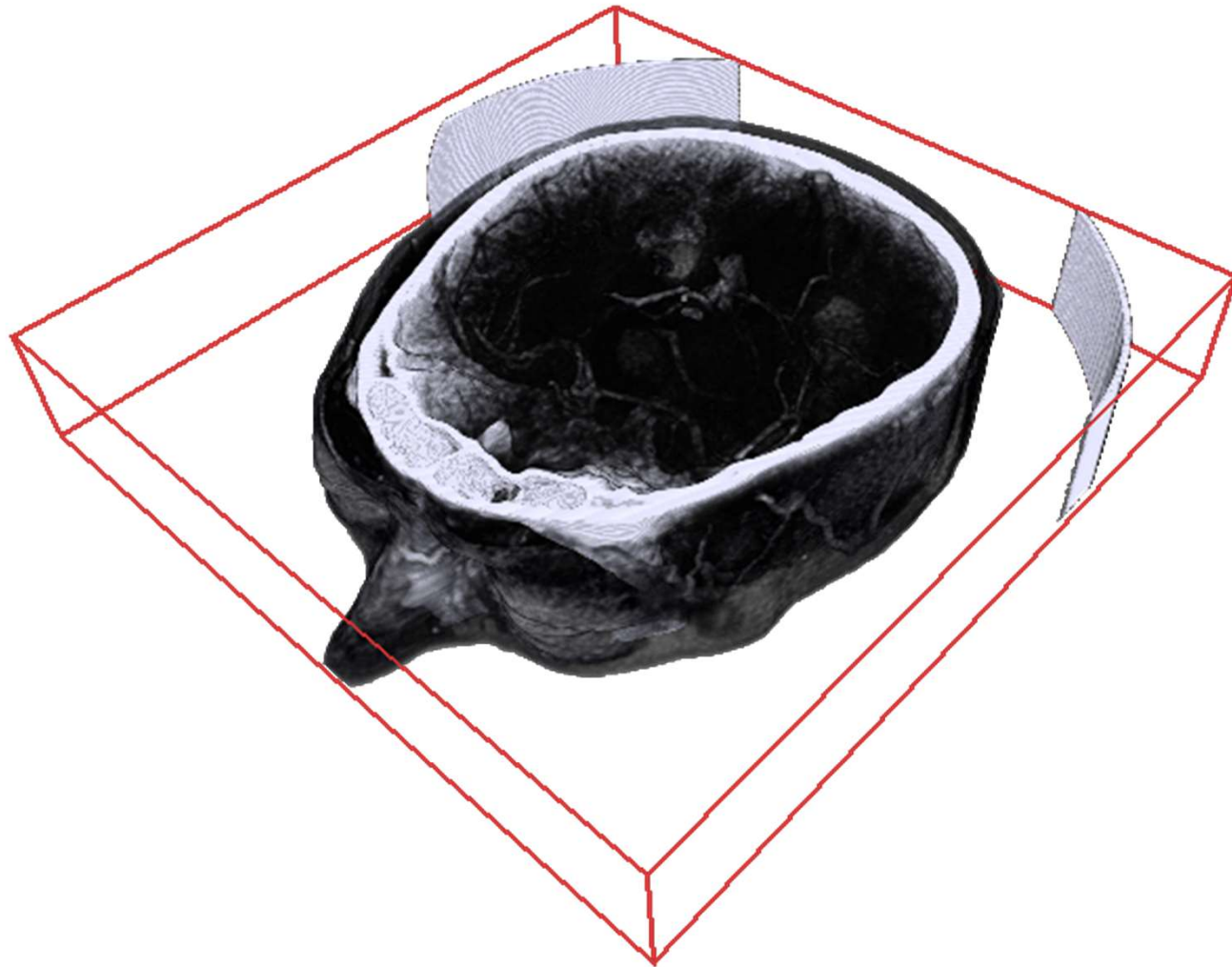
# Direct Volume Rendering



# Direct Volume Rendering

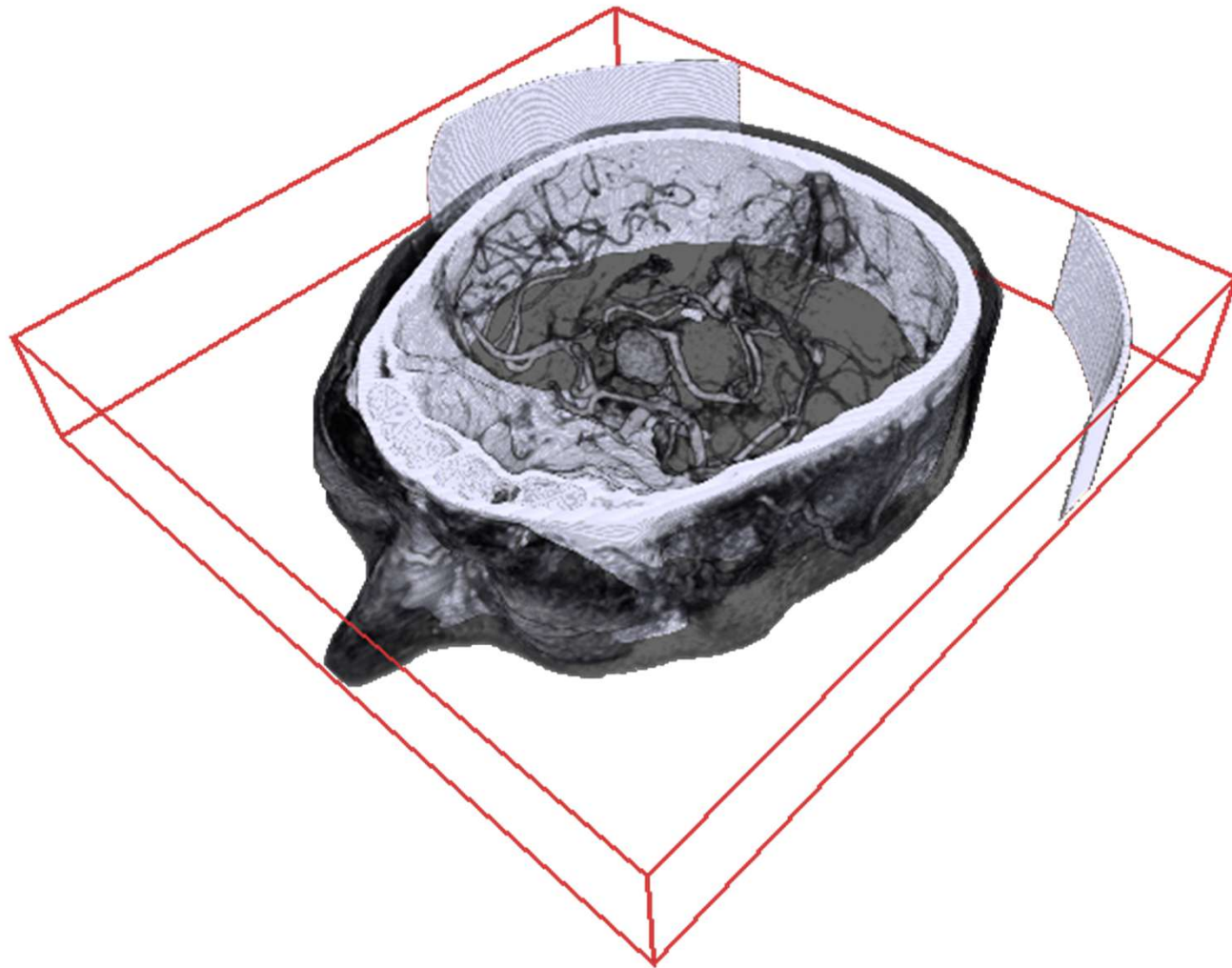


# Direct Volume Rendering

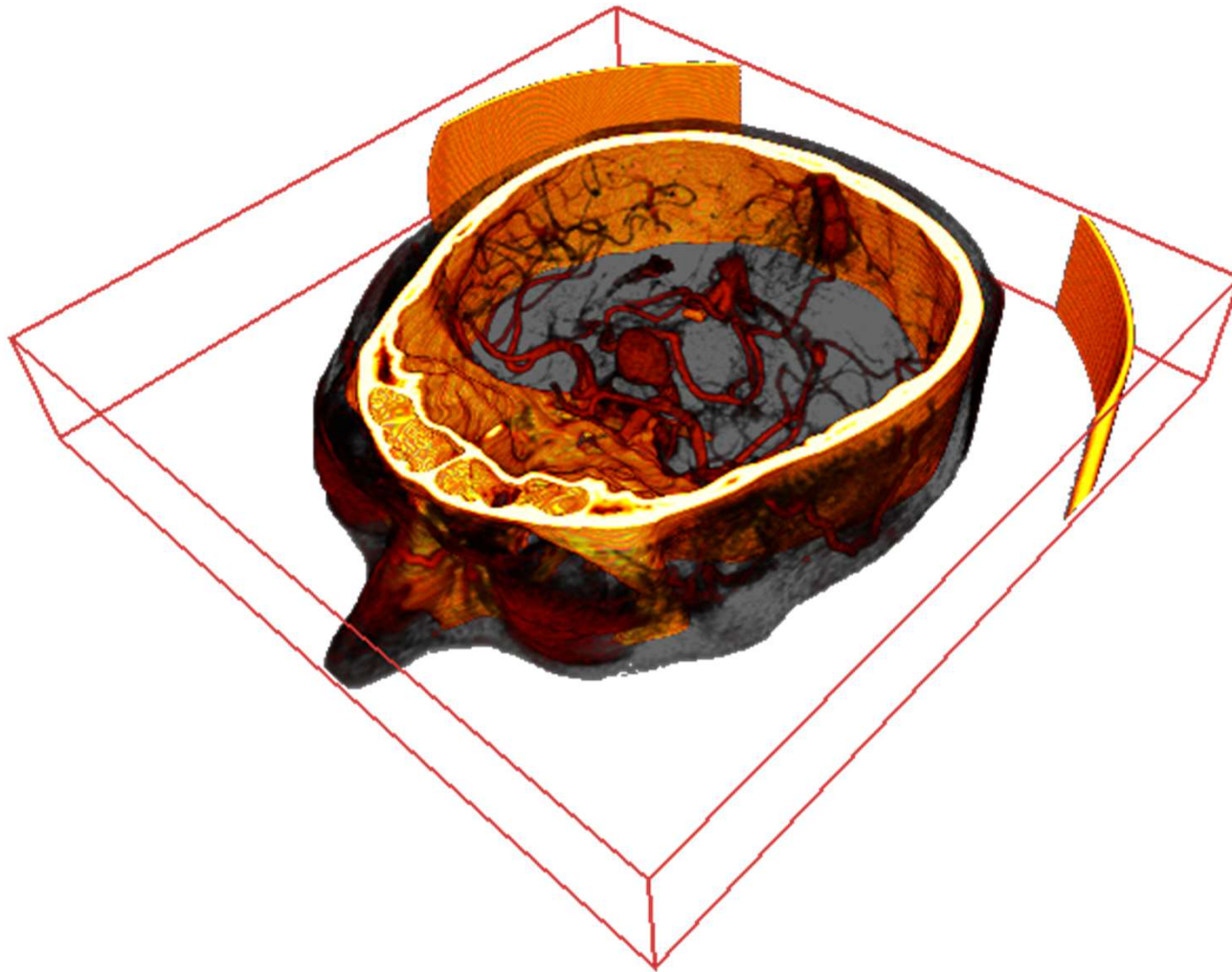




# Direct Volume Rendering



# Direct Volume Rendering

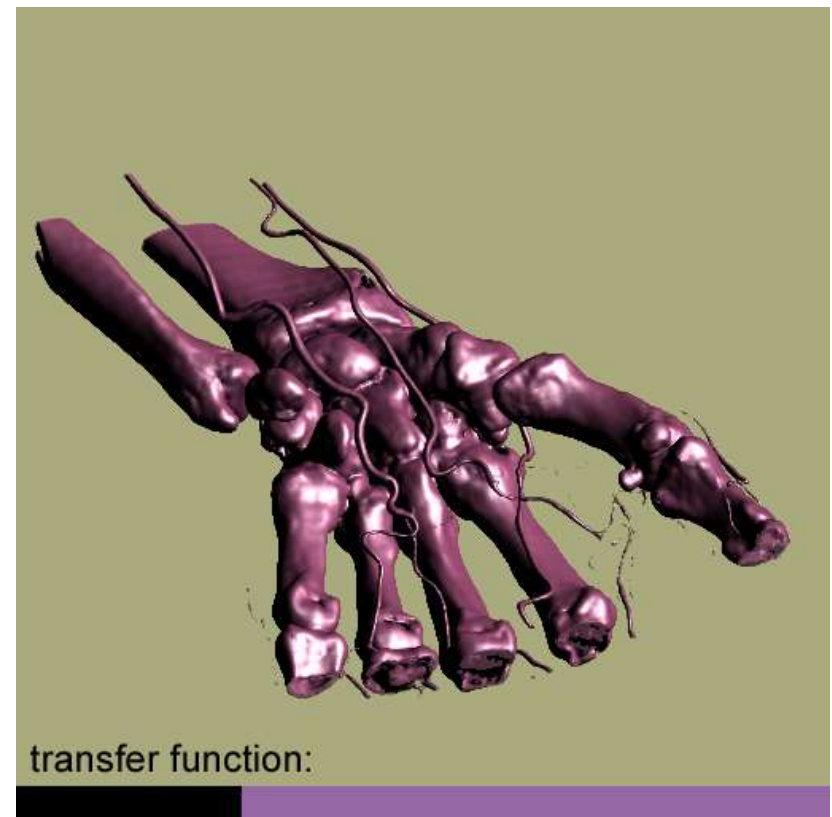
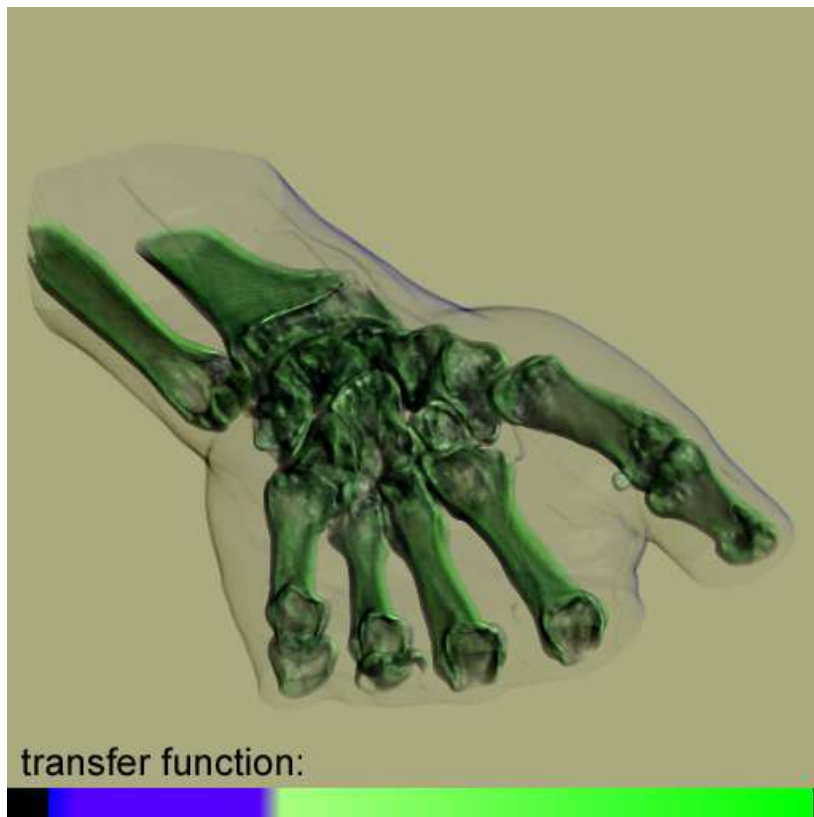


# Transparent Volumes vs. Isosurfaces



The *transfer function* assigns *optical properties* to data

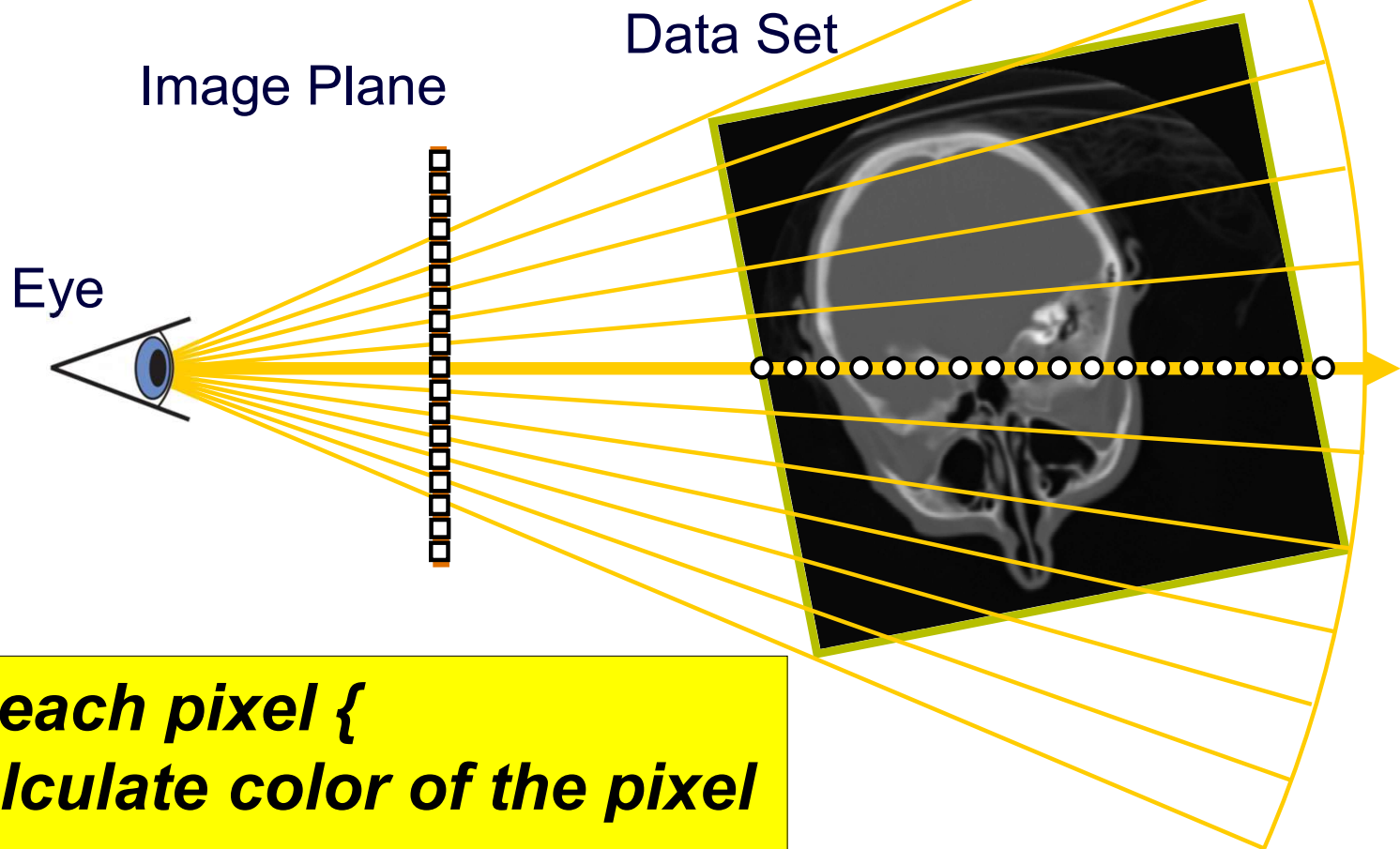
- Translucent volumes
- But also: isosurface rendering using step function as transfer function



# Direct Volume Rendering: Image Order



## *Image order approach:*

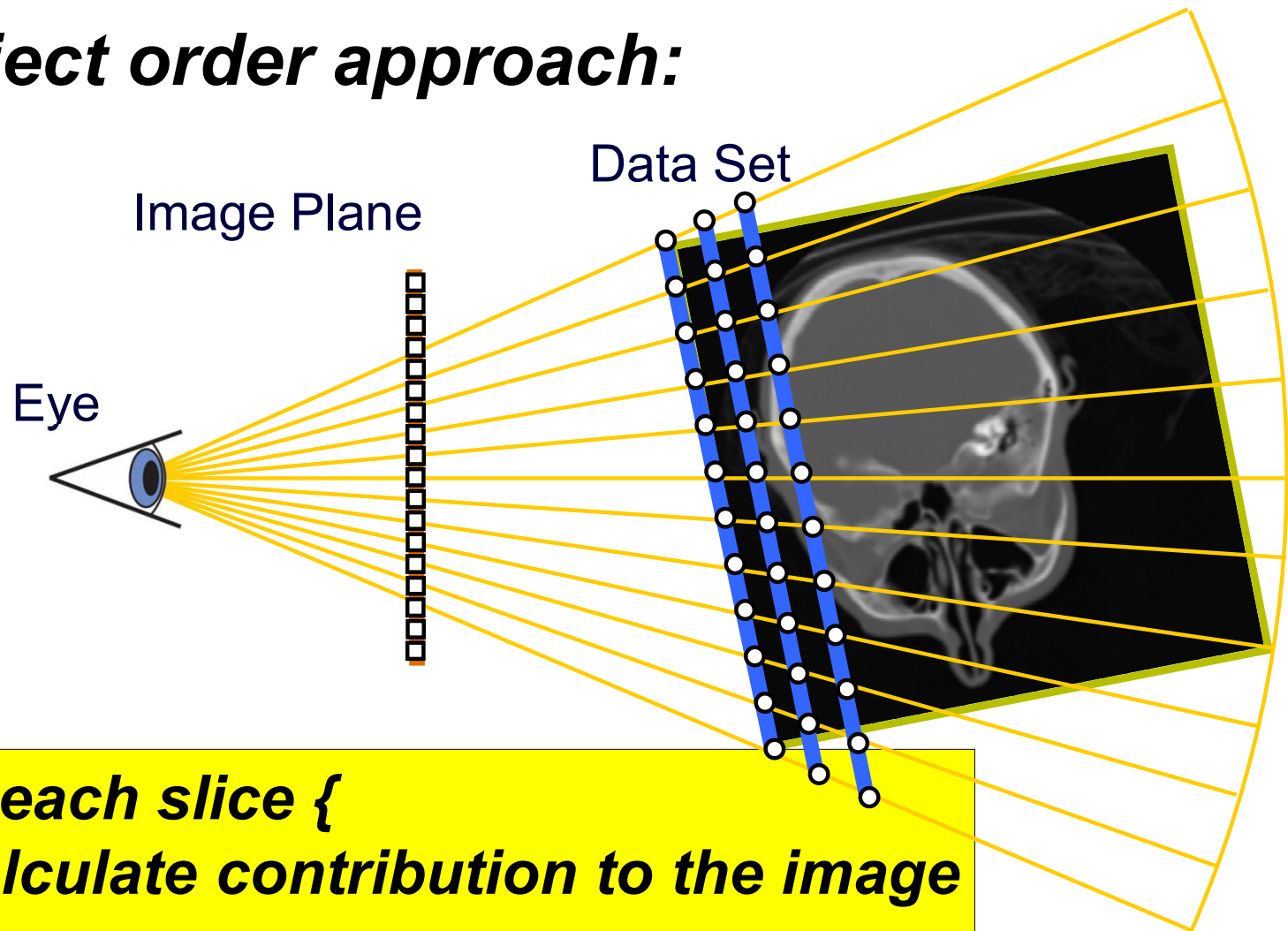


***For each pixel {  
    calculate color of the pixel  
}***

# Direct Volume Rendering: Object Order



## *Object order approach:*

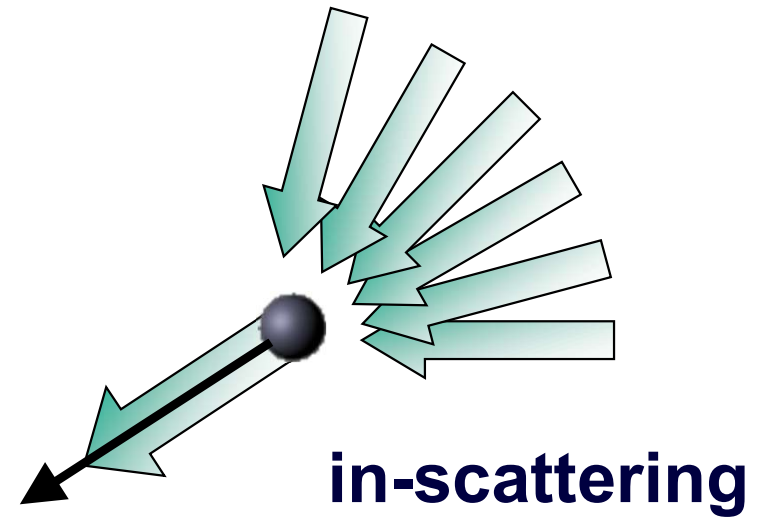
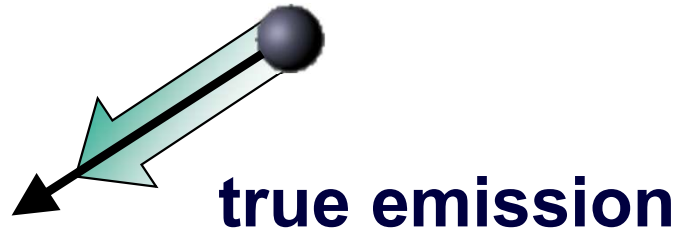


***For each slice {  
calculate contribution to the image  
}***

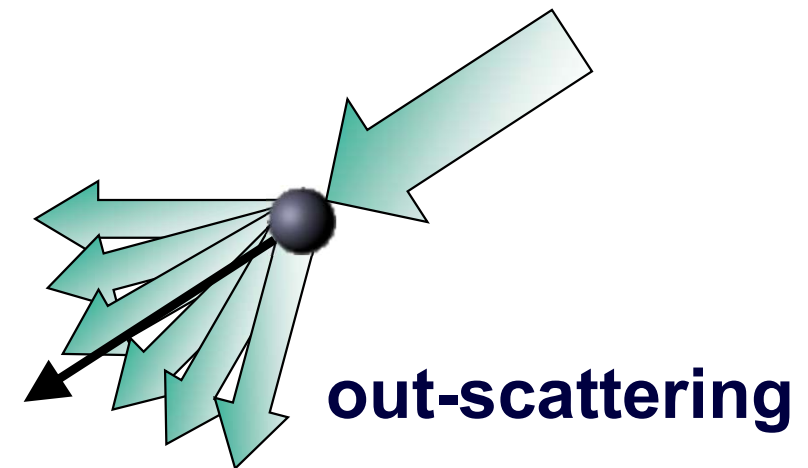
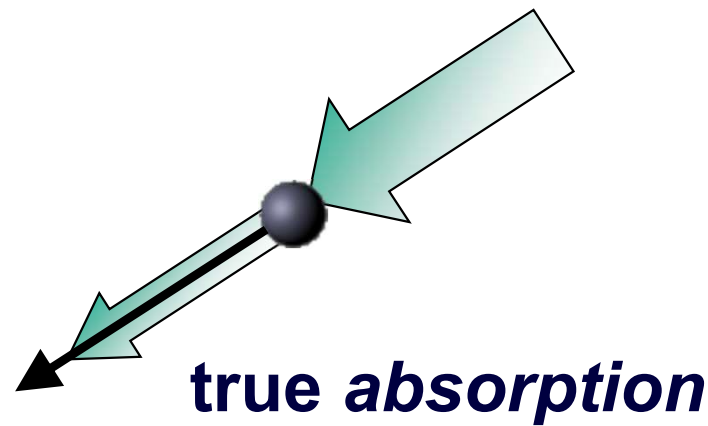
# Physical Model of Radiative Transfer



**Increase**



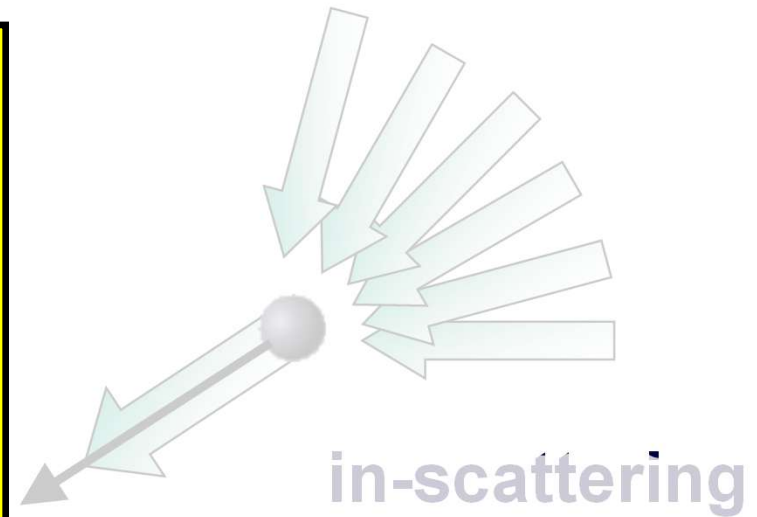
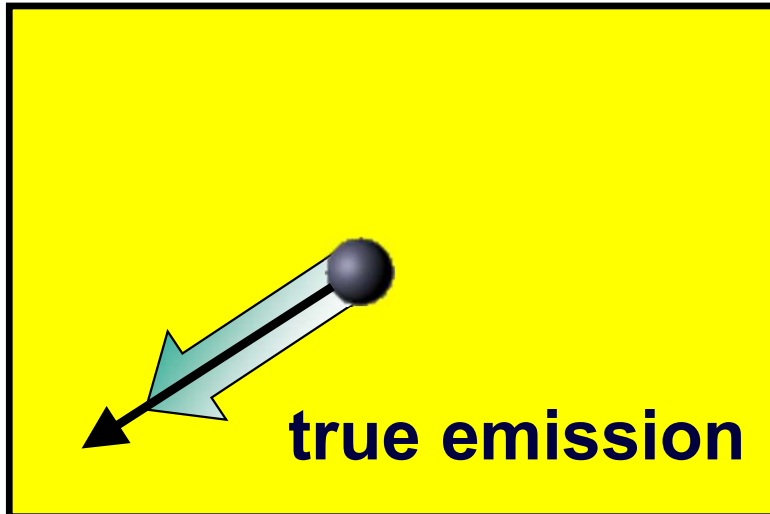
**Decrease**



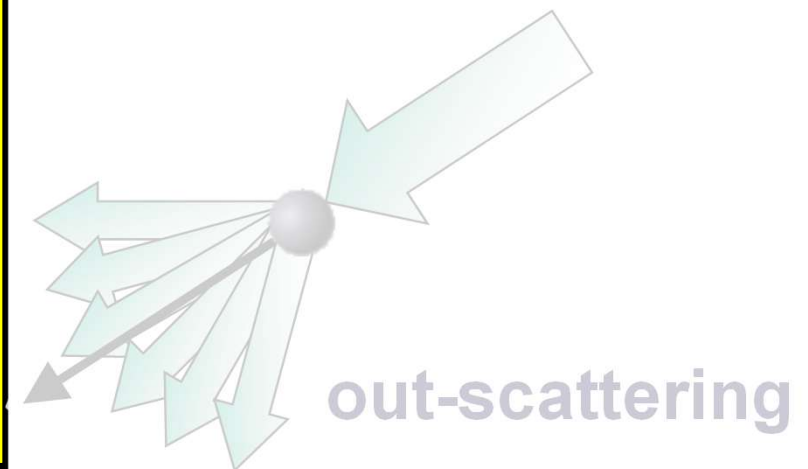
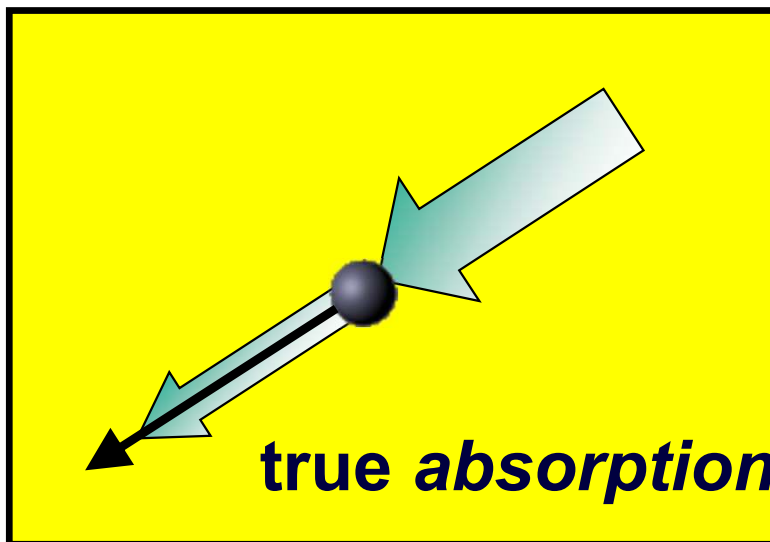
# Physical Model of Radiative Transfer



**Increase**



**Decrease**



# Optical Models: Physical Model gives ODE



Optical Models for Direct Volume Rendering, Nelson Max  
Emission-Absorption optical model

$$\frac{dI}{ds}(s) = q(s) - \kappa(s) I(s)$$



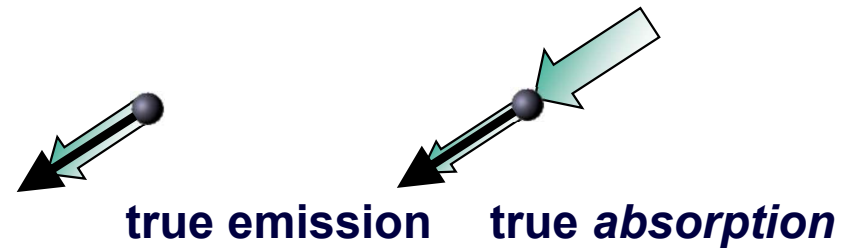
Right-hand side: *Rates of change* (derivatives) of light intensity along ray  
Absorption rate is proportional to light intensity: Solution is exponential



# Volume Rendering Integral



Volume rendering integral  
for *Emission Absorption* model



$$I(s) = I(s_0) e^{-\tau(s_0, s)} + \int_{s_0}^s q(\tilde{s}) e^{-\tau(\tilde{s}, s)} d\tilde{s}$$

$$\tau(s_1, s_2) = \int_{s_1}^{s_2} \kappa(s) ds.$$

Iterative/recursive numerical solutions:

***Back-to-front compositing***

$$C'_i = C_i + (1 - A_i)C'_{i-1}$$

***Front-to-back compositing***

$$C'_i = C'_{i+1} + (1 - A'_{i+1})C_i$$
$$A'_i = A'_{i+1} + (1 - A'_{i+1})A_i$$

here, all colors are *associated colors*!

# Thank you.

## Thanks for material

- Helwig Hauser
- Eduard Gröller
- Daniel Weiskopf
- Torsten Möller
- Ronny Peikert
- Philipp Muigg
- Christof Rezk-Salama