

KAUST

CS 247 – Scientific Visualization Lecture 15: Volume Visualization, Pt. 2

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Reading Assignment #8 (until Mar 26)



Read (required):

- Real-Time Volume Graphics, Chapter 4 (Transfer Functions) until Sec. 4.4 (inclusive)
- Paper:

Jens Krüger and Rüdiger Westermann, Acceleration Techniques for GPU-based Volume Rendering, IEEE Visualization 2003, http://dl.acm.org/citation.cfm?id=1081482

Volume Rendering





Volume rendering integral for *Emission Absorption* model



true emission true absorption

$$I(s) = I(s_0) e^{-\tau(s_0,s)} + \int_{s_0}^{s} q(\tilde{s}) e^{-\tau(\tilde{s},s)} d\tilde{s}$$

 $\tau(s_1, s_2) = \int_{s_1}^{s_2} \kappa(s) \, ds.$

Iterative/recursive numerical solutions:

Back-to-front compositing

$C'_i = C_i + (1 - A_i)C'_{i-1}$

here, all colors are *associated* colors!

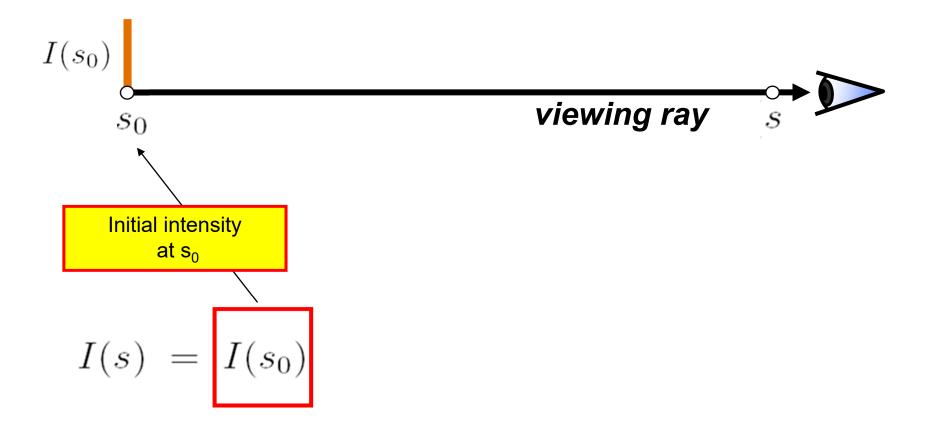
Front-to-back compositing

$$C'_{i} = C'_{i+1} + (1 - A'_{i+1})C_{i}$$

$$A'_{i} = A'_{i+1} + (1 - A'_{i+1})A_{i}$$

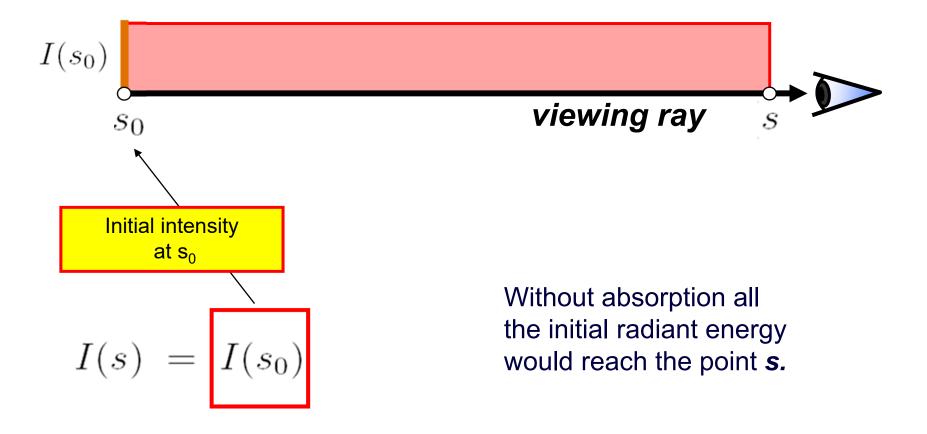


How do we determine the radiant energy along the ray? *Physical model:* emission and absorption, no scattering



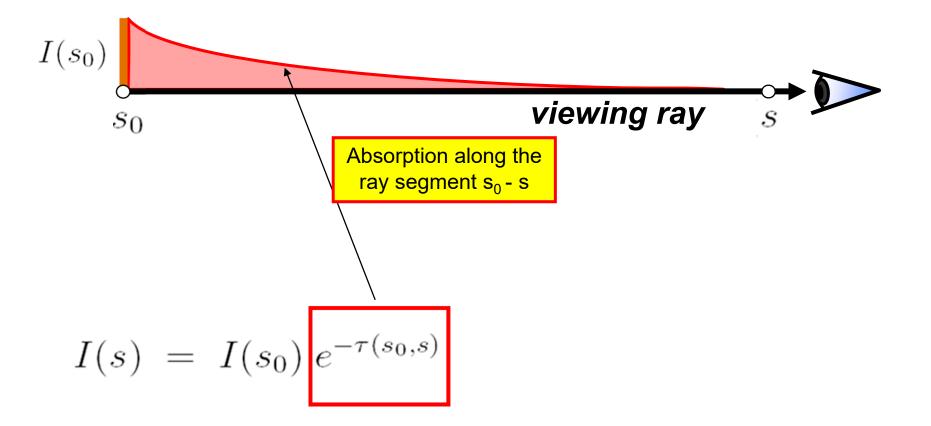


How do we determine the radiant energy along the ray?



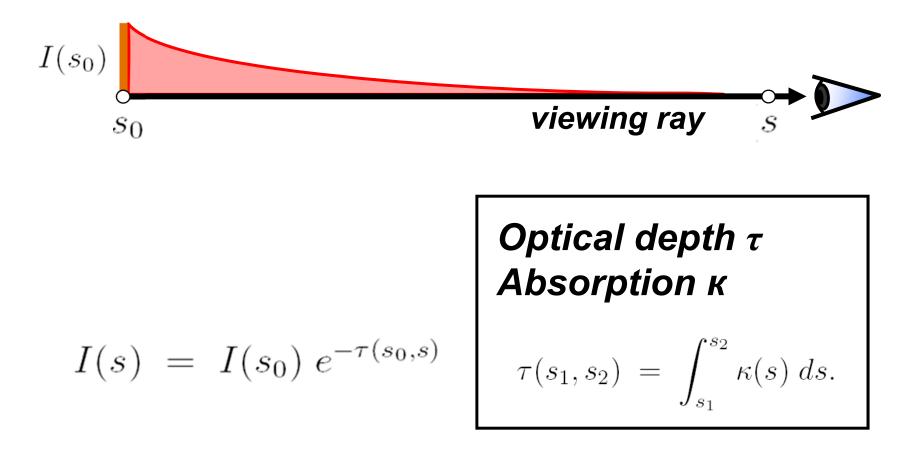


How do we determine the radiant energy along the ray?



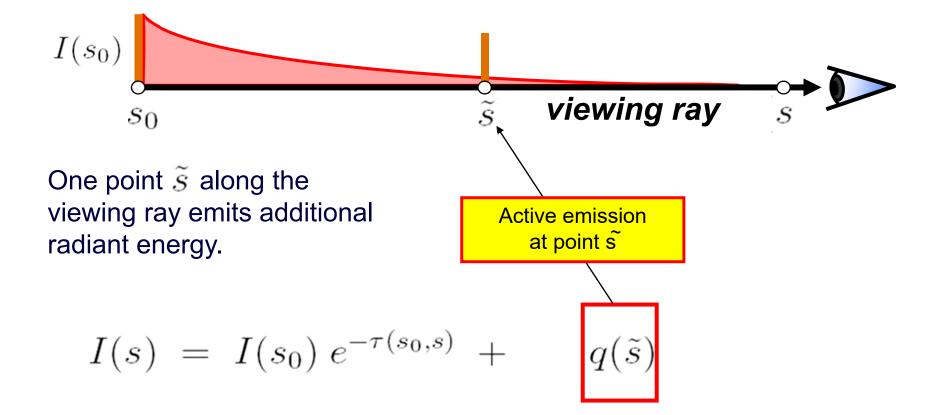


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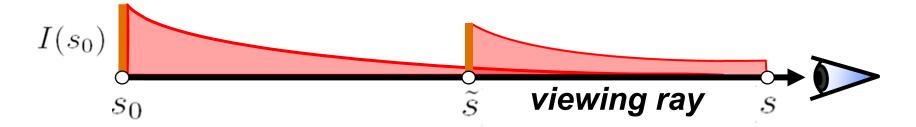
How do we determine the radiant energy along the ray?





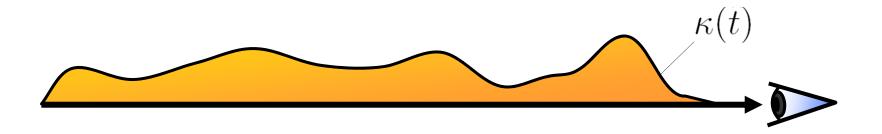
How do we determine the radiant energy along the ray?

Physical model: emission and absorption, no scattering



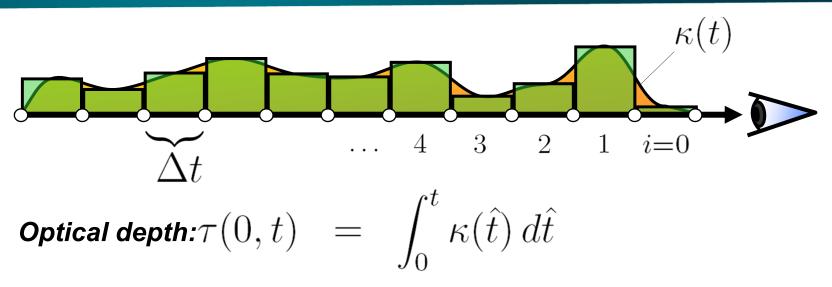
Every point \tilde{s} along the viewing ray emits additional radiant energy

$$I(s) = I(s_0) e^{-\tau(s_0,s)} + \int_{s_0}^{s} q(\tilde{s}) e^{-\tau(\tilde{s},s)} d\tilde{s}$$



Optical depth:
$$au(0,t) = \int_0^t \kappa(\hat{t}) d\hat{t}$$

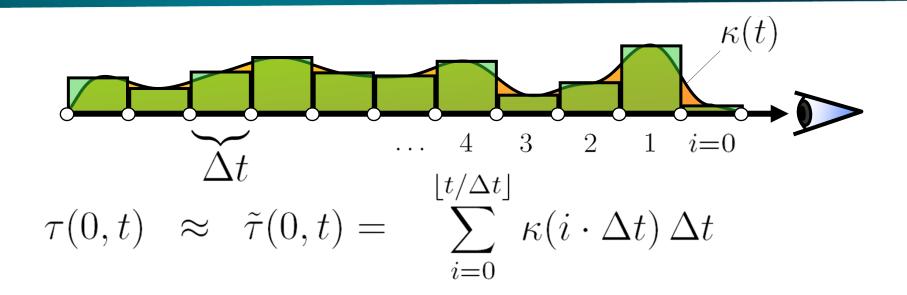




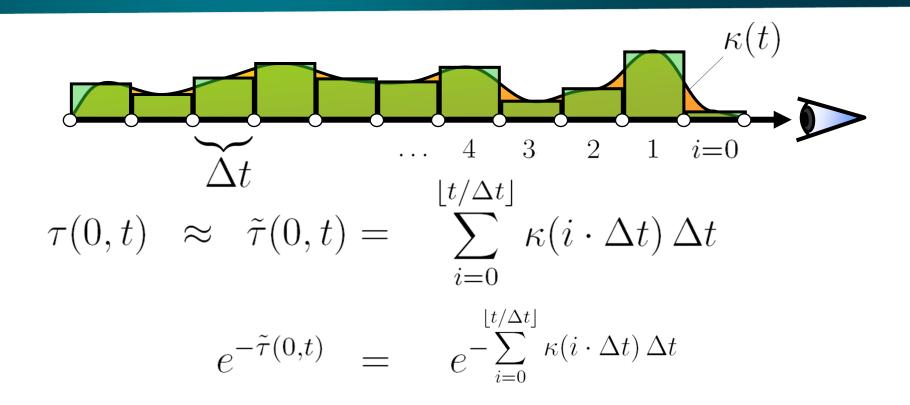
Approximate Riemann integral by Riemann sum:

$$\tau(0,t) \approx \sum_{i=0}^{\lfloor t/\Delta t \rfloor} \kappa(i \cdot \Delta t) \Delta t$$

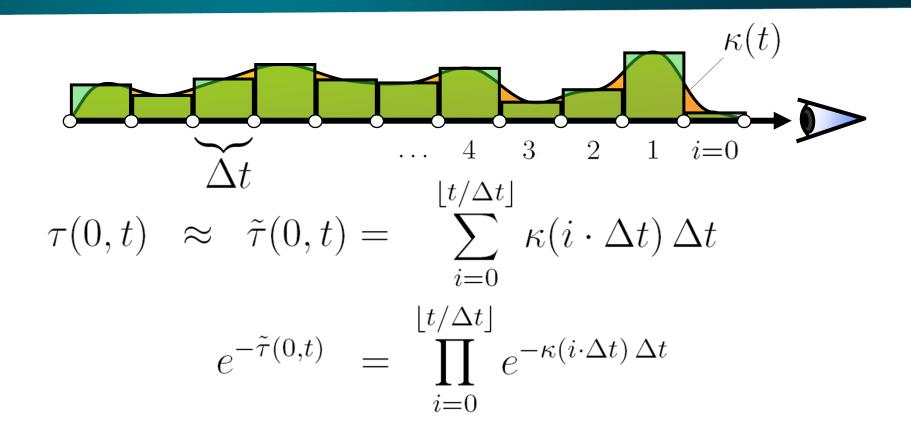




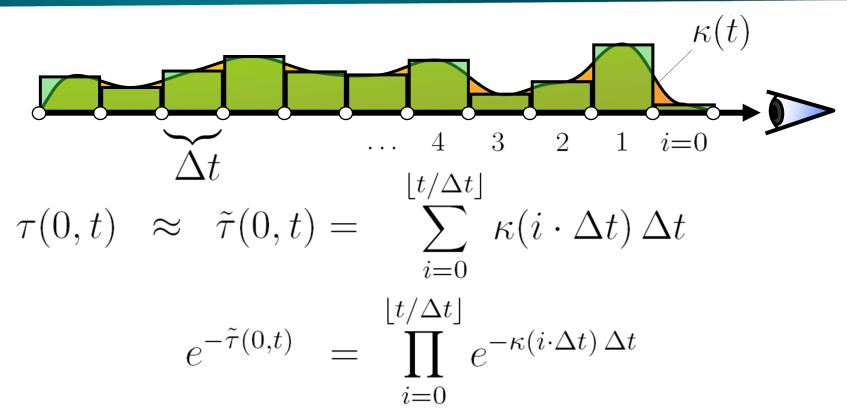






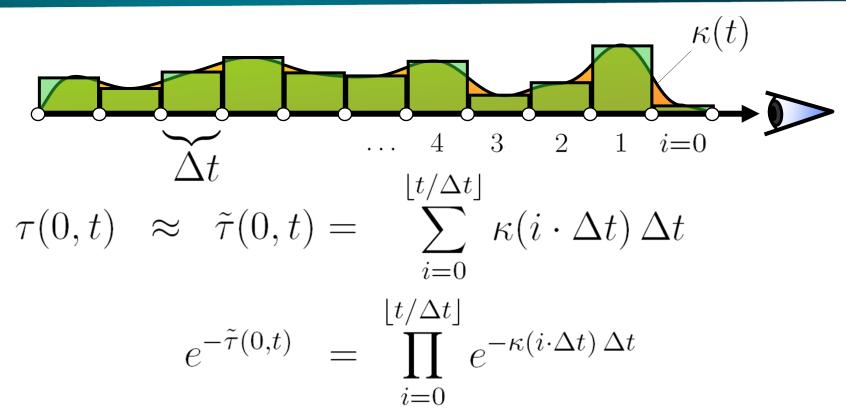






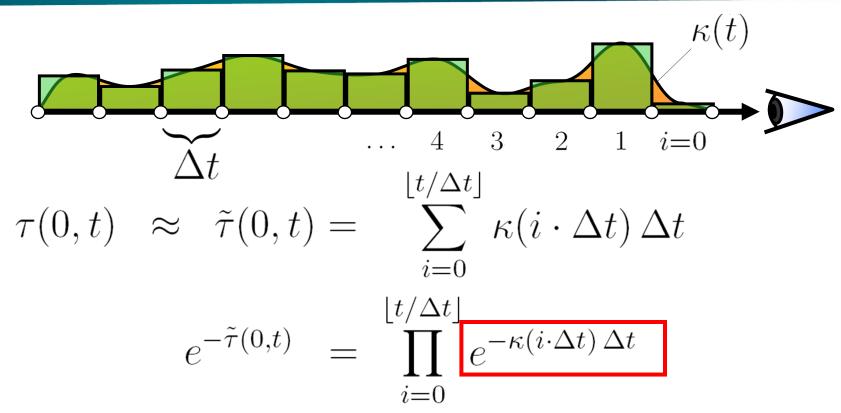
$$A_i = 1 - e^{-\kappa(i \cdot \Delta t) \,\Delta t}$$





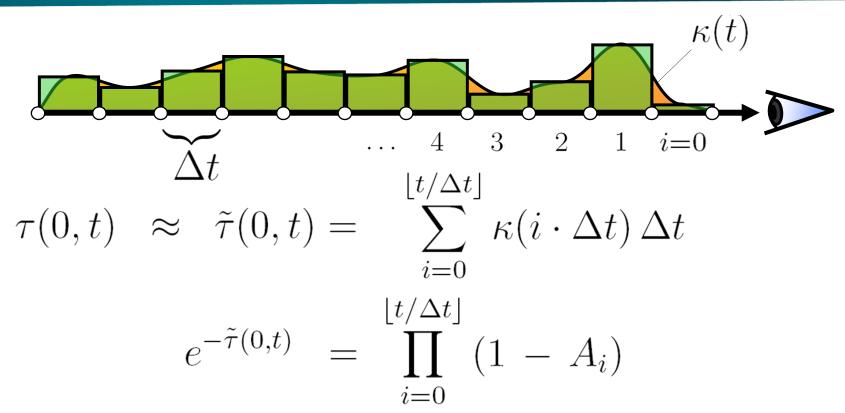
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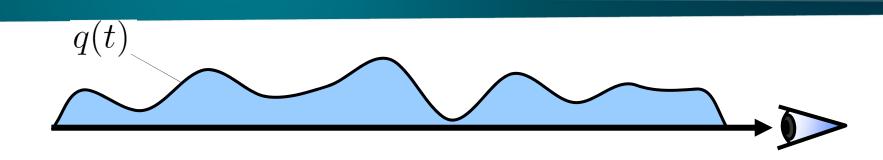


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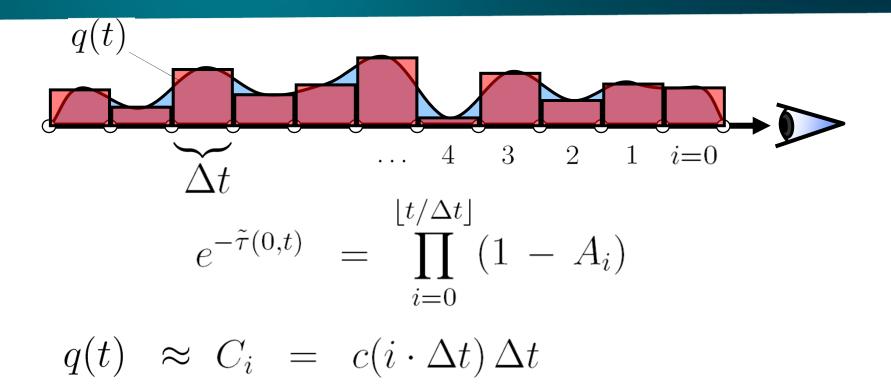




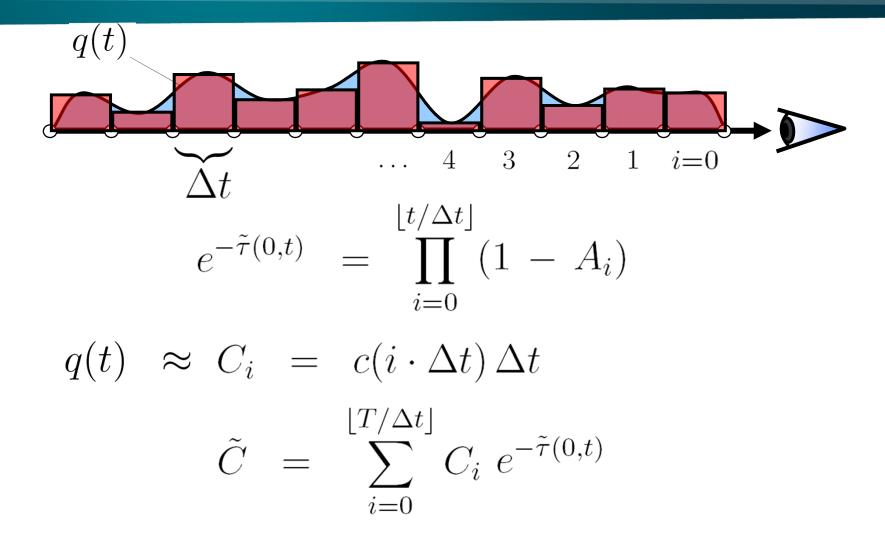
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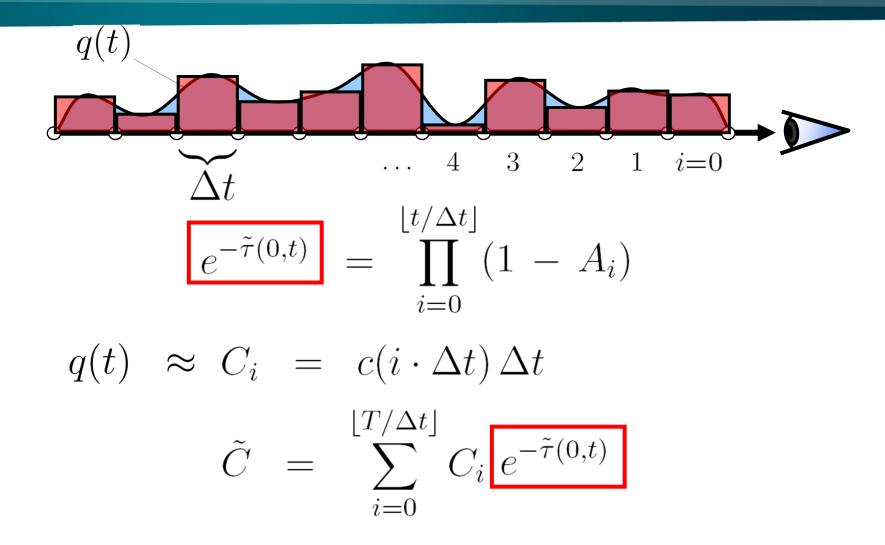




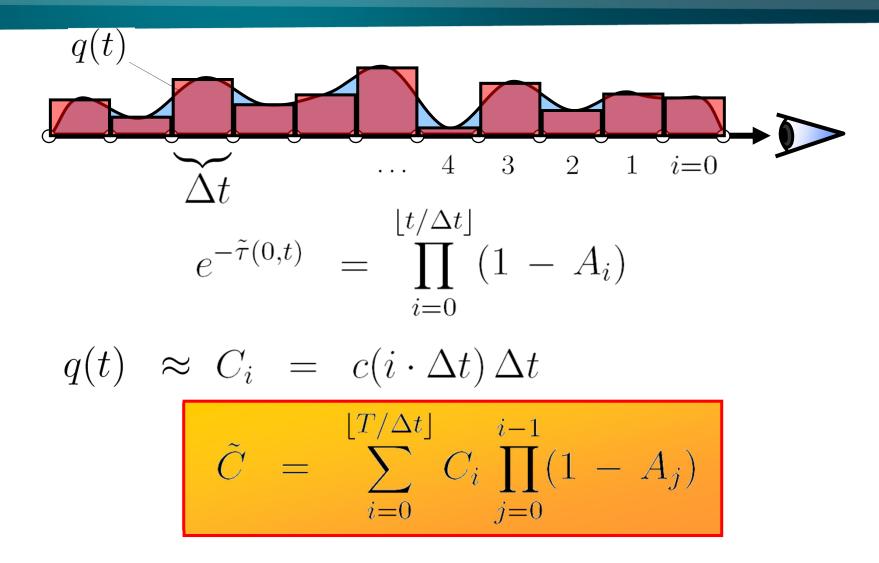




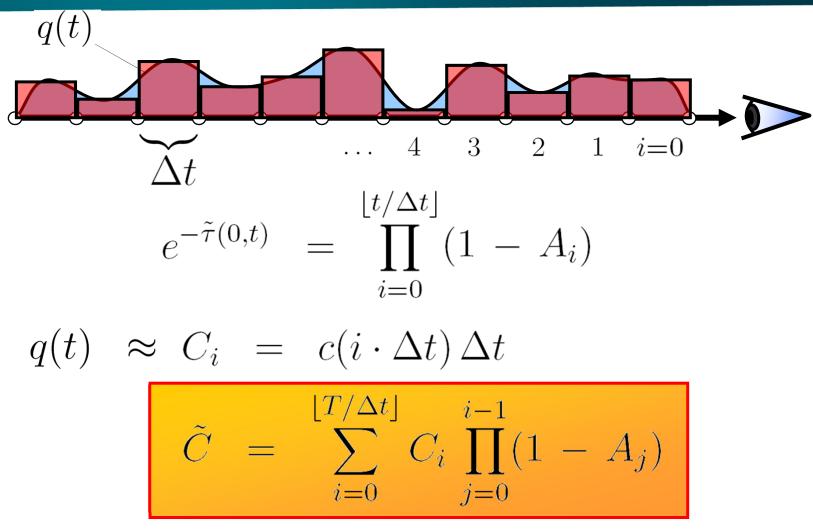






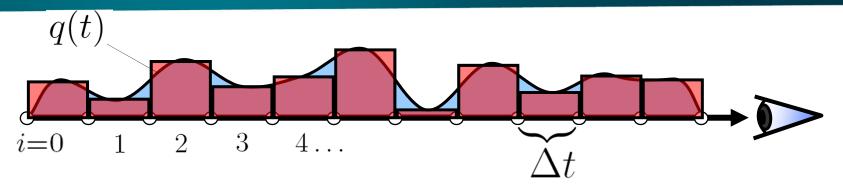






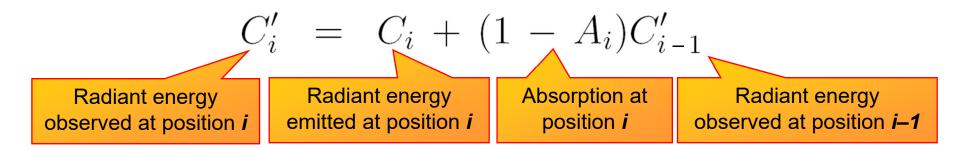
can be computed iteratively/recursively!



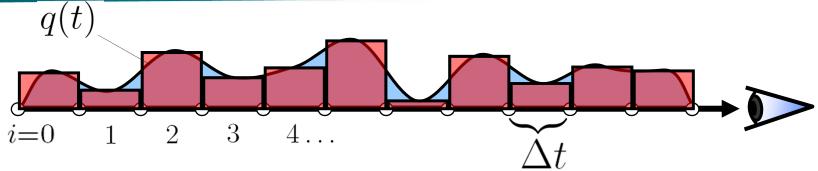


Note: we just changed the convention from i=0 is at the front of the volume (previous slides) to i=0 is at the back of the volume !

can be computed iteratively/recursively:







Back-to-front compositing

$$C'_i = C_i + (1 - A_i)C'_{i-1}$$

iterate from *i*=0 (back) to *i*=max (front): *i* increases

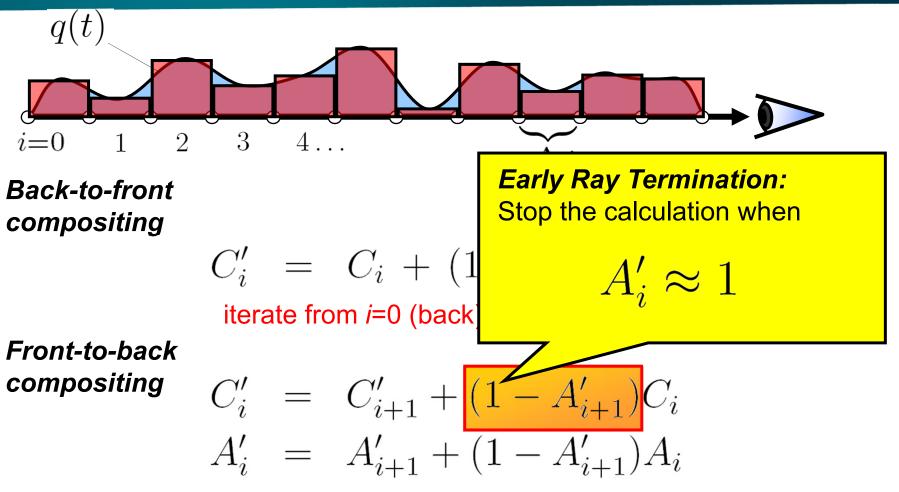
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iterate from *i*=max (front) to *i*=0 (back) : *i* decreases

Volume Rendering Integral Summary

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Thank you.

Thanks for material

- Helwig Hauser
- Eduard Gröller
- Daniel Weiskopf
- Torsten Möller
- Ronny Peikert
- Philipp Muigg
- Christof Rezk-Salama